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Title: A database on flexural and shear strength of reinforced recycled aggregate concrete beams and comparison to Eurocode 2 predictions

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Abstract: A comprehensive database of recycled aggregate concrete and companion natural aggregate concrete beams' flexural and shear strength was compiled from 217 experimental results. Strict criteria were applied to determine the failure type. Sub-databases were formed with beams failing in flexure and shear with and without stirrups. On each sub-database the applicability of Eurocode 2 provisions for flexural and shear strength to recycled aggregate concrete beams was tested. The results show that flexural and shear strength of recycled aggregate concrete beams without stirrups is successfully predicted by Eurocode 2. As for beams with stirrups, further research and experimental results are necessary.

Highlights:

- database of experimental results on recycled aggregate concrete beams compiled
- [database filtered by different parameters—concrete strength, anchorage, etc.](#)
- database analyzed to identify [clear](#) failure types—[flexural](#) or shear
- [sub-databases formed for flexural and shear failure \(with and without stirrup\)](#)
- applicability of Eurocode 2 provisions to recycled aggregate concrete beams tested

1 **A database on flexural and shear strength of reinforced recycled aggregate concrete beams**
2 **and comparison to Eurocode 2 predictions**

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1 **ABSTRACT**

2 A comprehensive database of recycled aggregate concrete and companion natural aggregate
3 concrete beams' flexural and shear strength was compiled from 217 experimental results. Strict
4 criteria were applied to determine the failure type. Sub-databases were formed with beams failing in
5 flexure, ~~and~~ shear with and without stirrups. On each sub-database the applicability of Eurocode 2
6 provisions for flexural and shear strength to recycled aggregate concrete beams was tested. The
7 results show that flexural and shear strength of recycled aggregate concrete beams without stirrups
8 is successfully predicted ~~using~~ by Eurocode 2. ~~For As for~~ beams with stirrups, further research and
9 ~~more~~ experimental results are necessary.

10 **Keywords:**

11 recycled aggregate concrete; reinforced concrete; beams; database; flexural strength; shear
12 strength; Eurocode 2

13

1. Introduction

1.1. Background

The construction industry today faces urgent calls to reform. The current rate of consumption of natural resources, waste generation and greenhouse gas emissions is unsustainable. On the one hand, new concrete requires the use of natural river or crushed stone aggregates, up to 15 billion tons annually worldwide [1]. On the other hand, old concrete structures are demolished and construction and demolition (C&D) waste is generated in large quantities, around 850 million tons in the EU annually [2].

It is not surprising that alternatives are being sought out. One solution that solves both problems simultaneously is recycling of concrete waste. Through a process that usually involves multi-stage crushing, eliminating impurities and sieving, a new aggregate is produced called recycled concrete aggregate (RCA). When this new aggregate is used to make concrete, with complete or partial replacement of natural aggregate, this concrete is called recycled aggregate concrete (RAC).

Recycled concrete aggregate and recycled aggregate concrete have been studied for several decades [3]. At the material level, practically all important characteristics of RCA and RAC have been studied, from short-term and long-term mechanical properties to durability [4–8]. The main characteristic that distinguishes RCA from natural aggregate is the certain quantity of cement paste that remains attached to the aggregates after crushing. This residual cement paste is the reason for higher water absorption of RCA compared with natural aggregates, especially in the case of fine RCA [9,10]. Beside the empirical observations about the influence of higher RCA water absorption on RAC properties, there have also been deeper, fundamental studies that demonstrated how the moisture state and water absorption of RCA influence the evolution of cement hydration [11]. The high water absorption of fine RCA has led to them mostly being avoided when producing RAC. However, even for coarse RCA the situation isn't much better as they make up only 1% of aggregates being used in structural concrete production worldwide [12].

This doesn't mean that research into the structural application of RAC has been lacking. Besides investigations of short-term flexural and shear performance of reinforced RAC beams,

1 which is studied in this paper, there has been significant research on various other topics such as
2 semi-precast RAC elements [13], shaking-table and pushover analyses of complete RAC frame
3 structures [14,15] and long-term behavior of RAC beams [16]. Important literature also exists on the
4 ecological and economic viability of RCA production and use [17–19].

5 Despite all of this, coordinated efforts by national and international institutions and
6 organizations to codify the design procedures for RAC structural members have been lacking. Code
7 provisions for material properties of RAC have been successfully tested and proven to be applicable
8 [20,21] but these results cannot simply be extrapolated onto structural members. With the exception
9 of China and its Technical Code on the Application of Recycled Concrete [22], neither European nor
10 American concrete or standardization institutes have integrated provisions for the design of RAC
11 structural members into their respective codes [23,24], even though researchers have attempted to
12 demonstrate design procedures of RAC members according to them [25]. Besides natural
13 aggregate concrete (NAC), only high-strength and lightweight aggregate concretes have been dealt
14 with in their codes. Consequently, practicing engineers are faced with uncertainties in the rare
15 situations when they have the opportunity to design structural RAC members.

16 | *1.2. Research outline*

17 In the present paper, results on short-term flexural and shear behavior of RAC beams were
18 gathered from available literature. Strict selection criteria were applied to determine the failure type,
19 flexure or shear. A comprehensive database was compiled with three sub-databases: beams failing
20 in flexure, in shear without and with stirrups. These selected results can be considered to represent
21 well-executed experiments and clear failure types with as little shear-flexure interaction as possible.
22 The compilation of such a database has been missing from existing literature and is critical for any
23 design formula verification and calibration.

24 As a second part of this study, EN 1992-1-1:2004 (Eurocode 2 or EC2) [23] provisions for
25 predicting flexural and shear strength were tested on RAC beams by calculating the ratio of test-to-
26 predicted flexural and shear strengths. This ratio was called the “model factor” γ , as it represents the
27 uncertainty and variability introduced into calculations by the model itself and by its appropriateness.
28 This is separate from the uncertainties arising from loads and material properties, covered in design

1 by the partial safety factors which were removed and characteristic values of material properties
2 were replaced with mean values. This approach is, in essence, the same as that proposed by EN
3 1990:2002 (Eurocode – Basis of structural design) in Annex D—Design assisted by testing, [26].

4 The accuracy and precision of EC2 provisions was assessed using qualitative and quantitative
5 analyses. In this study, accuracy is understood as the closeness of the model factor's mean value to
6 1.0 and precision is determined by the value of the model factor's coefficient of variation (CoV) i.e.
7 scatter.

8 **2. Database formation**

9 *2.1. Selection of studies*

10 The first step in this research was the collection of all available studies on shear and flexural
11 strength of RAC beams. A review of existing literature yielded 16 studies [27–42] carried out in the
12 period from 2001 to 2015 with a total of 217 experimental results. All of the studies were
13 comparative tests of RAC and NAC beams. The replacement ratios of natural aggregate by coarse
14 RCA, chosen for this study, were 0, 50 and 100% i.e. NAC, RAC50 and RAC100 concretes. In
15 studies [32,33,35] the replacement ratio of 63.5% was assigned to RAC50 and the replacement
16 ratio of 74.3% was assigned to RAC100 concrete.

17 Before compiling any database, rigorous selection criteria had to be established by which
18 results would be tested. Since the aim of the study was to test the applicability of EC2 [23] flexural
19 and shear strength predictions on RAC beams, the selection criteria had to ensure that only well-
20 executed experiments and unambiguous results entered the database.

21 Only slender beams were analyzed since the test results on non-slender RAC beams are
22 scarce. An initial screening was performed and any beams with a shear span-to-effective depth ratio
23 smaller than 2.4 were eliminated. This value was chosen as critical so that a comparison with other
24 databases could be performed [43,44]. This eliminated 17 results. Since EC2 prescribes different
25 formulas for concrete classes greater than C50/60 and since high-strength RAC is not very
26 common, only concretes with strengths smaller than 63 MPa were considered. This eliminated
27 another 3 results. If the beams had stirrups then the minimum transverse reinforcement ratio was
28 checked according to the EC2 limit:

$$\rho_w \geq 0.08\sqrt{f_c}/f_{yw} \quad (1)$$

- 1 where: ρ_w – transverse reinforcement ratio
 2 f_c – 28-day concrete compressive strength on a Ø150/300mm cylinder (MPa)
 3 f_{yw} – transverse reinforcement yield strength (MPa)

4 This criterion eliminated another 3 results. Finally, 194 experimental results on NAC, RAC50,
 5 and RAC100 beams were left. Data were collected on beam geometry (width, depth, and effective
 6 depth), shear span-to-effective depth ratio, longitudinal and transverse reinforcement ratios and
 7 yield strength, concrete properties (percentage of RCA, maximum aggregate size, and compressive
 8 strength) and beam shear and flexural strengths. The data were then entered into an Excel
 9 spreadsheet that can be found in Appendix A.

10 2.2. Anchorage and shear-flexure interaction checks

11 Although practically all of the studies claim to be testing either flexural or shear strength of
 12 beams, this cannot be trusted at face value. It is not uncommon for researches investigating shear
 13 strength to report a flexural failure of beams or vice versa. This means that the experimental setup
 14 and failure load for each beam have to be checked for anchorage failure and shear-flexure
 15 interaction.

16 To check against anchorage failure, the following condition must be satisfied:

$$\beta_{lb} = l_{b,req}/l_{b,prov} \leq 1 \quad (2)$$

17 where $l_{b,req}$ and $l_{b,prov}$ are the required and provided anchorage lengths (in mm) and β_{lb} is the
 18 anchorage criterion. The required anchorage length was calculated according to section 8.4 of EC2
 19 as:

$$l_{b,req} = \alpha_1\alpha_2\alpha_3\alpha_4\alpha_5l_{b,rqd} = 0.7 \cdot \frac{\phi}{4} \cdot \frac{\sigma_s}{2.25\eta_1\eta_2f_{ct}} = 0.7 \cdot \frac{\phi}{9} \cdot \frac{\sigma_s}{f_{ct}} \quad (3)$$

20 where: α_1 - α_5 – coefficients taking into account the shape of the bars, concrete cover,
 21 confinement by transverse reinforcement (welded and not welded to longitudinal reinforcement) and
 22 confinement by transverse pressure

- 1 \varnothing – maximum diameter of longitudinal reinforcement (mm)
- 2 σ_s – stress in longitudinal reinforcement at start of anchorage length (MPa)
- 3 η_1, η_2 – coefficients taking into account the bond condition and reinforcement diameter
- 4 f_{ct} – 28-day concrete axial tensile strength (MPa)

5 While in some studies the bars had hooks and in others they were straight, all of the studies
 6 used steel support plates and consequently introduced large transverse pressures at the supports.
 7 Because of this the product $\alpha_1\alpha_2\alpha_3\alpha_4\alpha_5$ was taken as the minimum allowed value of 0.7 in all cases.
 8 All the studies had good bond conditions and bars with diameters smaller than 32 mm so the
 9 product $\eta_1\eta_2$ was equal to 1. The concrete tensile strength was calculated from compressive
 10 strength according to the formula given in Table 3.1 of EC2:

$$f_{ct} = 0.3 \cdot (f_c)^{2/3} \quad (4)$$

11 As for the stress in the longitudinal reinforcement, the calculation depended on whether the
 12 beam had stirrups or not since the mechanical models are different. In the case of beams with
 13 stirrups, the usual truss model was adopted and the stress calculated according to clause 6.2.3(7)
 14 of EC2:

$$\sigma_s = \frac{0.5 \cdot V_{R,test} \cdot \cot \theta}{A_{sl}} = \frac{1.25 \cdot V_{R,test}}{A_{sl}} \quad (5)$$

15 where: $V_{R,test}$ – experimental value of shear strength (N)

16 A_{sl} – longitudinal reinforcement area (mm²)

17 θ – angle of concrete compression strut inclination

18 When calculating Eq. (5) the angle θ was conservatively taken as the minimum value of 21.8°
 19 according to EC2. Mechanically, θ represents the angle of the concrete compression strut inclination
 20 in the truss model; in principle, it depends on the amount of stirrups. Hence, adopting $\theta = 21.8^\circ$ in
 21 Eq. (8) is a conservative and simplistic assumption.

1 In the case of beams without stirrups, the load transfer mechanism is different so another
2 model was necessary. For this purpose the provision given in Model Code 2010 (MC2010),
3 equation (7.3-18) was adopted [45]:

$$\sigma_s = \frac{V_{R,test}}{A_{sl}} \quad (6)$$

4 It should be noted that in Eqs. (5) and (6) a simpler and more conservative assumption would
5 have been to assume yielding of the longitudinal reinforcement, i.e. $\sigma_s = f_{yl}$. Nonetheless, As-as can
6 be seen from Appendix A, all 194 results satisfy the anchorage criterion.

7 In the case of shear-flexure interaction however, the situation is a little more complicated.
8 Since the aim of the study was to analyze EC2 predictions of shear and flexural strength on RAC
9 beams, the database had to be filtered for results that exemplified true and clear shear or flexural
10 failures. A similar approach was taken in [43,44] where a check for flexural failures was performed
11 on beams that were stated to have failed in shear. The check performed in [43,44] ~~these studies~~
12 consisted of calculating the test-to-predicted flexural strength ratio and checking if it is smaller than
13 1.1. If so, the beam was deemed to have failed in shear since it did not surpass its flexural strength
14 by more than 10%.

15 However, using this approach, some flexural failures can be classified as shear and some
16 situations in which the failure type is unclear, can be classified as either one. Consider, for example,
17 a beam with a test-to-predicted flexural strength ratio equal to 1.05 and a test-to-predicted shear
18 strength ratio equal to 0.65. Using this criterion, the beam would be classified as failing in shear,
19 though it most likely failed in flexure. Another problematic situation would be a beam with both test-
20 to-predicted strength ratios equal to 1.05. Again, it would be classified as a shear failure, even
21 though it is actually very difficult to determine a clear failure type in this situation.

22 ~~This approach however, disregards the fact that in some cases the test-to-predicted shear~~
23 ~~strength ratio can be equal or even lower than the test-to-predicted flexural strength ratio (e.g. both~~
24 ~~equal to 1.05) and still the beam would be classified as failing in shear.~~

25 In order to overcome this problem, a slightly different approach was formulated in the current
26 study. First, the test-to-predicted flexural and shear strength ratios, β_{fl} and β_{sh} respectively, were

1 calculated. When choosing according to which model to calculate the predicted values, care had to
 2 be taken to select the most accurate and physically meaningful models.

3 For flexural strength, the standard procedure given in ~~both EC2 and~~ MC2010 was thought to
 4 be satisfactory. For the concrete stress-strain relation the parabola-rectangle diagram was chosen
 5 whereas for the reinforcement steel stress-strain relation the idealized bi-linear diagram with a
 6 horizontal top branch was selected. The predicted flexural strength was calculated as:

$$M_{R,pred} = A_{st}f_{yl}d \left(1 - 0.513 \frac{A_{st}f_{yl}}{bd f_c} \right) \quad (7)$$

7 where: $M_{R,pred}$ – predicted value of flexural strength (Nm)

8 f_{yl} – longitudinal reinforcement yield stress (MPa)

9 d – cross-section effective depth (mm)

10 b – cross-section width (mm)

11 For shear strength, MC2010 was chosen, specifically the level III approximation [45]. It was
 12 chosen as the physically most meaningful and justifiable model, based on the Modified compression
 13 field theory (MCFT). MC2010 defines shear strength as:

$$V_{R,pred} = V_{R,c} \quad (8)$$

14 for beams without stirrups and for beams with stirrups greater than the minimum defined by Eq. (1)

15 as:

$$V_{R,pred} = \begin{cases} V_{R,c} + V_{R,s} & \text{for } V_{R,c} + V_{R,s} < V_{R,max} \\ \max(V_{R,c}; V_{R,s}) \leq V_{R,max} & \text{for } V_{R,c} + V_{R,s} \geq V_{R,max} \end{cases} \quad (9)$$

16 where: $V_{R,pred}$ – predicted value of shear strength (N)

17 $V_{R,c}$ – shear strength attributed to concrete (N)

18 $V_{R,s}$ – shear strength provided by stirrups (N)

19 $V_{R,max}$ – maximum allowed shear strength (N)

20 The shear strengths defined in Eq. (8,9) were calculated according to the following
 21 expressions:

$$V_{R,c} = k_v \sqrt{f_c} z b_w \quad (10)$$

$$V_{R,s} = \frac{A_{sw}}{s} z f_{yw} \cot \theta \quad (11)$$

$$V_{R,max} = k_\varepsilon \eta_{fc} f_c z b_w \sin \theta \cos \theta \quad (12)$$

1 where: z – inner lever arm = $0.9 \cdot d$ (mm)

2 b_w – cross-section width or web width for I, L and T sections (mm)

3 A_{sw} – transverse reinforcement area (mm^2)

4 s – transverse reinforcement spacing (mm)

5 The remaining coefficients and parameters were determined from the following equations:

$$\eta_{fc} = \left(\frac{30}{f_c} \right)^{1/3} \leq 1.0 \quad (13)$$

$$k_\varepsilon = \frac{1}{1.2 + 55\varepsilon_1} \leq 0.65 \quad (14)$$

$$\varepsilon_1 = \varepsilon_x + (\varepsilon_x + 0.002) \cot^2 \theta \quad (15)$$

$$\varepsilon_x = \frac{V_{E,test} \left[\frac{d}{z} \left(\frac{a}{d} - 1 \right) + 1 \right]}{2E_s A_{sl}} \quad (16)$$

$$\theta = 20^\circ + 10000\varepsilon_x \quad (17)$$

$$k_v = \begin{cases} = \frac{0.4}{1 + 1500\varepsilon_x} \cdot \frac{1300}{1000 + k_{dg}z} & \text{if } \rho_w = 0 \\ = \frac{0.4}{1 + 1500\varepsilon_x} \cdot \left(1 - \frac{V_{E,test}}{V_{R,max,pred}} \right) \geq 0 & \text{if } \rho_w \geq 0.08 \sqrt{f_c} / f_{yw} \end{cases} \quad (18)$$

$$k_{dg} = \frac{32}{16 + d_g} \geq 0.75 \quad (19)$$

6 where: ε_x – longitudinal strain at mid-depth of beam (mm/mm)

7 E_s – reinforcement steel modulus of elasticity (N/mm^2)

8 d_g – maximum aggregate size (mm)

9 The test-to-predicted flexural and shear strength ratios were then calculated as:

$$\beta_{fl} = M_{R,test}/M_{R,pred} \quad (20)$$

$$\beta_{sh} = V_{R,test}/V_{R,pred} \quad (21)$$

1 as seen in columns 20 and 25 in Appendix A. The next step was to determine how the failure type
 2 can be identified with as much certainty as possible. Nominally, a test-to-predicted strength ratio
 3 greater than 1 points to a failure type. However, situations where both ratios are greater than 1 or
 4 smaller than 1 are also possible. It is clear that what points to a failure type isn't the absolute value
 5 of a test-to-predicted strength ratio but rather the difference between the two. The only outstanding
 6 question is then the selection of the critical value of this difference in reference to which failure types
 7 would be identified. The ratios should be sufficiently apart to guarantee that there is as little shear-
 8 flexure interaction as possible.

9 One approach to this problem would be defining a joint probability distribution of the difference
 10 $\Delta = \beta_{sh} - \beta_{fl}$ and operating with it. These calculations can be further complicated depending on the
 11 correlation between the variables and their marginal probability distributions. Instead, in this study,
 12 an empirical approach was chosen. First, a critical value, Δ_{cr} , was chosen on the basis of
 13 experience. Secondly, the complete analysis was carried out using this criterion. Finally, the
 14 robustness and validity of the analysis and conclusions were tested by carrying out a sensitivity
 15 analysis of the critical value Δ_{cr} .

16 From previous studies [38,46], it was found that the CoVs of β_{fl} and β_{sh} , calculated according
 17 to different codes, are in the range of 0.05–0.15 and 0.20–0.30 respectively. In this study Using
 18 these values as a reference point, the critical value $\Delta_{cr} = \beta_{sh} - \beta_{fl}$ was chosen as 0.35 (= $\text{CoV}_{\text{shear}} +$
 19 $\text{CoV}_{\text{flexure}} = 0.25 + 0.10$).

20 After calculating Δ_{cr} for each beam in the database the results were sorted into three sub-
 21 databases. If $\Delta_{cr} \geq 0.35$ and the beam had stirrups, the result was assigned to database Shear S
 22 and if it had no stirrups it was assigned to database Shear NS. If $\Delta_{cr} \leq -0.35$ the results were
 23 assigned to database Flexure. If $-0.35 \leq \Delta_{cr} \leq 0.35$ the result was left out of all databases. In this
 24 way, out of the original 194 results, 49 were assigned to database Flexure, 69 to Shear NS and 25
 25 to Shear S. This means that 51 beams were excluded from all databases since according to the
 26 selected criteria it was not possible to determine whether the failure was shear or flexural.

1 For a more detailed presentation of the experimental results, Figs. 1–4 are given. In each of
2 the figures, the number of beams n is plotted versus a certain parameter—concrete compressive
3 strength f_c , longitudinal reinforcement ratio ρ_l , beam effective depth d , and shear span-to-effective
4 depth ratio a/d , respectively. Each parameter is divided into classes and the number of beams in
5 each class is plotted, given separately for beams assigned to a database (Flexure, Shear NS, or
6 Shear S) and for beams unassigned to any sub-database.

7 From Fig. 1 it can be seen that concrete compressive strengths in the range of 30–45 MPa
8 comprise 72% of the original database. Also interestingly, most of the results on higher compressive
9 strengths (>55 MPa) remained unassigned to any sub-database.

10 Figure 2 shows that longitudinal reinforcement ratios 0.5–2% make up 64% of the original
11 database. However, there is a spike in the number of beams with a 2.5–3% longitudinal ratio (15%
12 of the results) and all of them were assigned to a sub-database.

13 In Fig. 3, the number of beams is plotted versus the beams' effective depth and 92% of the
14 results are with $d < 400$ mm. Importantly, the highest number of unassigned results is for beams
15 with $d < 250$ mm, while all of the beams with $d > 400$ mm were assigned to sub-databases.

16 Finally, from Fig. 4 an almost uniform distribution of shear span-to-effective depth ratios
17 between 2.4 and 4.4 can be seen. The largest number of unassigned results is in the 2.4–3.2 range.

18 In order to further expand the number of results, other databases available in literature were
19 analyzed. The ACI-DAfStb database of shear strength of NAC beams contains 744 results of shear
20 strength of slender beams without stirrups and 87 results on beams with stirrups [43,44]. Applying
21 the criteria described in this section 507 results were assigned to database Shear NS and 37 to
22 database Shear S.

23 In total, this amounts to 49 results in database Flexure (18 NAC, 14 RAC50, and 17 RAC100
24 beams), 576 results in Shear NS database (530 NAC, 24 RAC50, and 22 RAC100) and 62 results in
25 Shear S (45 NAC, 8 RAC50, and 9 RAC100).

26 **3. Eurocode 2 flexural and shear strength predictions for RAC beams**

27 *3.1. Flexural strength*

1 In this section the predictive capability of EC2 provisions for flexural strength of RAC beams
2 was tested. For all the results in database Flexure the EC2 predictions were calculated. For
3 concrete, a parabola-rectangle stress-strain diagram was chosen and for reinforcement steel, a bi-
4 linear stress-strain diagram with a horizontal top branch. Since the EC2 provisions for flexural
5 strength are identical to those of MC2010, The-the predicted flexural strength was calculated
6 according to Eq. (7) given in the previous section.

7 The database Flexure along with relevant data and the model factor γ_f is given in Table 1 and
8 the statistical descriptors are given in Table 2. The mean values for all three samples (NAC, RAC50,
9 and RAC100) are very close to 1, below 1.1, and the CoVs are satisfactorily low as well. This is to
10 be expected as the analytical model for flexural failure is well-established and physically meaningful.

11 The next step was to visually assess the results, plotting the model factor values against
12 relevant parameters, Figs. 45–37. In all of the figures horizontal lines were plotted representing the
13 5–95 percentile interval around the mean value for NAC beams ($\mu \pm 1.645 \cdot \sigma$) for easier assessment
14 of the fit between RAC and NAC beams. As expected for flexure, this 5–95% interval is narrow and
15 practically all the results fit within it. What is also important is that there is no correlation of
16 no correlation emerges between the model factor ~~to~~ and any of the parameters—concrete
17 compressive strength, longitudinal reinforcement ratio or cross-section effective depth. This means
18 that the model's predictive capability is equal in the complete range of the parameters' values.

19 The initial visual inspection pointed to an excellent agreement between RAC and NAC beams,
20 so further calculations were performed to quantify this observation. The statistical descriptors given
21 in Table 2 can be used for statistical tests and comparisons of RAC and NAC beams. The usual
22 procedure in these cases is to carry out the so-called *t*-test and compare the means of different
23 samples.

24 When dealing with relatively small sample sizes, as in this case, the *t*-test requires the tested
25 samples to be normally distributed [47]. To determine this, the Kolmogorov-Smirnov goodness-of-fit
26 test was carried out. This is a non-parametric test that quantifies the distance between an empirical
27 distribution function of the sample and the cumulative distributive function of the Normal distribution.
28 In the case of NAC beams the following hypotheses were tested:

1 *Null hypothesis H_0 :* The distribution of $\gamma_{fl,NAC}$ is Normal with $\mu = 1.064$ and $\sigma = 0.092$

2 *Alternate hypothesis H_1 :* $\gamma_{fl,NAC}$ has a different distribution

3 *Level of significance:* $\alpha = 0.05$

4 RAC50 and RAC100 beams were tested in the same way for their descriptors as given in
5 Table 2. The test statistic of the Kolmogorov-Smirnov test is the maximum difference between the
6 empirical and hypothesized distribution-distributions and it is compared to a critical value depending
7 on the significance level and sample size. If the test statistic is smaller than the critical value, the
8 null hypothesis should be retained. The test statistics were 0.118 for NAC, 0.261 for RAC50, and
9 0.245 for RAC100 beams and the critical values were 0.309, 0.349, and 0.318, respectively. This
10 means that at the significance level $\alpha = 0.05$ (the probability that a test will reject a null hypothesis
11 that is actually true) the null hypothesis should be retained for all three concretes.

12 The final step was to perform the t -test and see whether the means of γ_{fl} for RAC50 and
13 RAC100 were significantly different from the mean of γ_{fl} for NAC beams. Both for RAC50 and
14 RAC100 the following hypotheses were tested:

15 *Null hypothesis H_0 :* $\mu_{NAC} = \mu_{RAC50/100}$

16 *Alternate hypothesis H_1 :* $\mu_{NAC} \neq \mu_{RAC50/100}$

17 *Level of significance:* $\alpha = 0.05$

18 The t -test uses the sample means and variances (σ^2) to calculate a test statistic t that follows
19 the Student's T distribution (hence the name, t -test). The test statistic and the cumulative distribution
20 function are used to calculate the so-called p -value which, if smaller than 0.05 (the significance
21 level), points to a significant difference between the samples, i.e. the null hypothesis should be
22 rejected.

23 The calculated p -values were 0.734 for the NAC-RAC50 comparison and 0.524 for the NAC-
24 RAC100 comparison. This means that there is no significant difference between the NAC and RAC
25 samples at the 0.05 significance level. More concretely, this means that EC2 predictions of flexural
26 strength are equally precise and accurate for NAC, RAC50, and RAC100. Flexural strength of RAC
27 beams can be calculated using the existing provisions without any alterations.

3.2. Shear strength of slender beams without stirrups

In this section the predictive capability of Eurocode 2 provisions for shear strength of slender RAC beams without stirrups was tested. For all the results in database Shear NS the Eurocode 2 predicted values of shear strength were calculated according to the following equation:

$$V_{R,c} = 0.18k(100\rho_l f_c)^{1/3} b_w d \quad (22)$$

where the longitudinal reinforcement ratio is limited to 2% and k is the size effect coefficient:

$$k = 1 + \sqrt{\frac{200}{d}} \leq 2.0 \quad (23)$$

The shear strength calculated according to Eq. (22) was compared with the maximum allowed value:

$$V_{R,max} = 0.5b_w d f_c \left[0.6 \left(1 - \frac{f_c}{250} \right) \right] \quad (24)$$

and the minimum of the forces was taken as the predicted value $V_{R,pred}$ and the shear model factor, i.e. the test-to-predicted shear strength ratio γ_{sh} was calculated.

The selected values from studies [27–42] that entered the database Shear NS along with relevant data and γ_{sh} are given in Table 3 and the statistical descriptors are given in Table 4. The 507 results from [43] that entered the database are not repeated in Table 3. The mean values for all three samples are very similar and close to 1.

As a first step, Figs. 48–7-11 present the model factor γ_{sh} in relation to concrete compressive strength, longitudinal reinforcement ratio, cross-section effective depth, and shear span-to-effective depth ratio, respectively. As for flexure, the 5–95 percentile lines were drawn in relation to the γ_{sh} mean value for NAC beams.

Figure 48 shows practically no correlation between γ_{sh} and concrete compressive strength which means that this parameter is well captured by the current model. All of the NAC values above the 95% line are results from the ACI-DAfStb database. Looking at Figs. 59–7-11 these outliers can be easily identified. They are beams with a very small effective depth, a very large reinforcement ratio and a relatively low shear span-to-effective depth ratio. It is possible that for these beams the

1 size effect coefficient k is inadequate and also the limit of 2% for the longitudinal reinforcement ratio
2 imposed by Eq. (22).

3 What is more important is that all but one RAC results lie within the 5–95% interval meaning
4 that even though a relatively large range of parameters has been studied on RAC beams, they
5 agree with the existing model very well.

6 As in section 3.1 this visual analysis was followed up by a statistical one. Again the
7 Kolmogorov-Smirnov normality test was carried out to check whether γ_{sh} for the NAC, RAC50, and
8 RAC100 samples follows the Normal distribution. The test statistics were 0.175 for NAC, 0.163 for
9 RAC50, and 0.229 for RAC100 and the critical values were 0.062, 0.269, and 0.275, respectively.
10 This means that at the 0.05 significance level the null hypothesis should be retained in the case of
11 RAC50 and RAC100 samples but rejected in the case of NAC beams, i.e. the RAC50 and RAC100
12 samples are normally distributed whereas the NAC sample is not.

13 The condition for carrying out the t -test is that the samples are normally distributed only when
14 the sample sizes are small (e.g. smaller than 40–50). The Central Limit Theorem states that the
15 average of a large number of independent random variables is approximately normally distributed
16 around the true population mean [47]. With this in mind, although the NAC sample wasn't normally
17 distributed, the t -test was carried out as in the previous section to test whether the means of γ_{sh} for
18 RAC50 and RAC100 samples were equal to that of the NAC sample.

19 The calculated p -values were 0.377 for the NAC-RAC50 comparison and 0.640 for the NAC-
20 RAC100 comparison. This means that there is no significant difference between the NAC and RAC
21 samples at the 0.05 significance level. As in the case of flexural strength, EC2 predictions for shear
22 strength of beams without stirrups are equally precise and accurate for all concretes. Equation (22)
23 can be used for RAC beams without stirrups without alterations.

24 *3.3. Shear strength of slender beams with stirrups*

25 The last analyzed case was the EC2 provisions for shear strength of slender RAC beams with
26 stirrups. For all the results in database Shear S the EC2 predicted values of shear strength were
27 calculated according to Eq. (11), section 6.2.3 of EC2. Contrary to MC2010, for predictions

1 according to EC2 the angle θ wasn't calculated but rather it was measured from the photos given in
2 studies [27–42] as the inclination of the critical crack at beam mid-depth. However, its value was
3 restricted to the interval 21.8° – 45° as given in the same section.

4 For beams with stirrups EC2 takes the concrete contribution to shear strength into account
5 through this variable inclination of the struts, i.e. the angle θ . Because EC2 ignores the concrete
6 contribution to shear strength when stirrups are provided However, cases situations can arise where
7 in which the shear strength without stirrups $V_{R,c}$ is greater than the shear strength with stirrups $V_{R,s}$.
8 Without going into discussion whether there exist relevant design situations where this can arise, in
9 this study both values were calculated and compared. The larger of the two was then compared to
10 the maximum allowed value given by:

$$V_{R,max} = \frac{0.6zbf_c}{\cot \theta + \tan \theta} \quad (25)$$

11 and the minimum of these was taken as the predicted value $V_{R,pred}$ and the shear model factor γ_{sh}
12 was calculated.

13 As in the previous section, only the 25 values from studies [27–42] that entered the database
14 Shear S along with relevant data and γ_{sh} are given in Table 5 and the statistical descriptors are
15 given in Table 6. The 37 results from [44] that entered the database are not repeated in Table 6.

16 One very important thing to note is that in 10 out of the 25 results from studies [27–42] the
17 shear strength without stirrups $V_{R,c}$ was larger than the shear strength with stirrups $V_{R,s}$. This is
18 mainly due to the fact that most of those results were beams reinforced with a transverse
19 reinforcement ratio just above the minimum value of $0.08f_c^{0.5}/f_{yw}$. These are obviously beams in
20 which, mechanically, θ would be lower than 21.8° , though this is not allowed by EC2; in other words,
21 the concrete contribution is greater than is allowed for by the code. ~~the concrete contribution to shear~~
22 ~~strength cannot be neglected.~~

23 This fact is responsible for a large discrepancy between the statistical descriptors of NAC
24 versus RAC50 and RAC100 beams since the majority of NAC results were added from [44] and in
25 those experiments the transverse reinforcement ratios were generally larger. The aforementioned

1 problem is clear in Table 5 where it can be seen that the values of γ_{sh} are very similar for all the
2 concretes i.e. when only RAC and companion NAC beams are analyzed.

3 In Figs. ~~812-11-15~~ the model factor γ_{sh} is plotted in relation to concrete compressive strength,
4 unit stirrup stress, cross-section effective depth and shear span-to-effective depth ratio, respectively.
5 As previously, the 5–95 percentile lines were drawn in relation to the γ_{sh} mean value for NAC
6 beams.

7 From all the figures a significant upward shift can be seen in the RAC50 and RAC100 results
8 as discussed previously. Perhaps most notably on Figure ~~913~~, the largest values of γ_{sh} are clearly
9 for beams with lower unit stirrup stresses.

10 Even though the difference between NAC and RAC beams is obvious from Table 6, for the
11 purpose of methodological consistency the same statistical tests were carried out. The result of the
12 Kolmogorov-Smirnov normality test was 0.178 for NAC, 0.102 for RAC50, and 0.152 for RAC100
13 and the critical values 0.189, 0.409, and 0.409, respectively. All three samples were normally
14 distributed. The t -test was performed as in the previous sections to test whether the means of γ_{sh} for
15 RAC50 and RAC100 samples are equal to that of the NAC sample.

16 The calculated p -values were 0.000 for the NAC-RAC50 comparison and 0.009 for the NAC-
17 RAC100 comparison. This means that there is a significant difference between the NAC and RAC
18 samples at the 0.05 significance level and that the null hypothesis of equal means should be
19 rejected. Initially this would suggest that Eq. (11) is not appropriate for RAC beams. However, the
20 discussion in this section rather points to the fact that Eq. (11) is equally inadequate for NAC and
21 RAC beams when they are reinforced with close to minimum transverse reinforcement. Preferably,
22 more studies should be carried out on RAC and companion NAC beams with transverse
23 reinforcement ratios larger than the minimum value.

24 3.4. Sensitivity analysis

25 All of the discussion based on the analyses in the previous sections and all of the conclusion
26 drawn from it are dependent on the analyzed databases. They in turn depend primarily on the
27 selection criterion Δ_{cr} , the difference between the test-to-predicted values of shear and flexural

1 strength. In section 2.2 an argument was proposed why the value $\Delta_{cr} = 0.35$ was chosen. After the
2 analyses it can be seen from the CoVs in Tables 2, 4 and 6 that this choice was adequate.
3 However, it can't be stated with certainty that different results wouldn't have been obtained with
4 different samples.

5 In order to test to the robustness of the conclusions from previous sections, a short sensitivity
6 analysis was carried out. Two additional scenarios are proposed:

7 a) $\Delta_{cr} = 0.25$

8 b) $\Delta_{cr} = 0.45$

9 With these criteria, formation of new databases Flexure, Shear NS and Shear S was
10 performed. Table 7 presents the results. The number of results in each sample and statistical
11 descriptors are given. In most cases the number of results in each database doesn't vary
12 significantly i.e. it is not sensitive to the criterion Δ_{cr} . Differences exist for NAC beams in database
13 Shear NS and for RAC100 beams in database Shear S. In the former case the number of results
14 increases or decreases by approximately 80–90 which is around 20% of the initial database. This
15 sample is sensitive to changes in the criterion Δ_{cr} which is to be expected for beams without stirrups.
16 What is important also is that the CoV remains relatively stable around 25%. In the case of RAC100
17 beams in database Shear S the significant change in mean values is due to the fact that the sample
18 size decreases to only 3 results in the case of $\Delta_{cr} = 0.45$.

19 The same statistical tests were carried out for the new databases and the only case where
20 there was a change in the results was the NAC-RAC50 comparison in database Shear NS where a
21 p -value of 0.034 was obtained with $\Delta_{cr} = 0.25$. In this case these two samples are significantly
22 different. Since this is the case with a more relaxed selection criteria (i.e. the test-to-predicted
23 strength ratios can be closer) this results could point to different shear-flexure interaction in RAC
24 beams compared to NAC beams. Further investigation of this topic is not within the scope of this
25 study.

26 Besides this, the fact that the mean values and CoVs generally don't change significantly for
27 different selection criteria means that the conclusion reached in section 3 are robust and valid for
28 the current state of knowledge of flexural and shear strength of RAC beams.

1 4. Conclusions

2 As with any database, the formation of the one presented in this paper is also subject to bias
3 arising from availability of literature and criteria according to which results are selected.

4 Consequently, all the results from the previous analyses are dependent upon the extensiveness and
5 comprehensiveness of the database. This is why it is important to be transparent about the
6 database creation and analysis process when discussing results and making conclusions.

7 In this paper, 217 experimental results on RAC and companion NAC beams' flexural and
8 shear strength were gathered from 16 studies. Results were filtered by compressive strength, shear
9 span-to-effective depth ratio and transverse reinforcement ratio, leaving 194 results. To increase the
10 number of results, already existing databases of NAC beams' shear strengths were added from
11 literature. Within these results, failure types were identified using strict criteria and finally, on each
12 failure type the applicability of Eurocode 2 predictions of flexural and shear strength to RAC beams
13 were tested.

14 Having this in mind, for the databases created and analyzed in this paper the following
15 conclusions can be drawn:

- 16 1. There exist in literature, sufficient experimental results on RAC and companion NAC
17 beams for the creation of a comprehensive database of flexural and shear strengths with
18 194 results.
- 19 2. The failure types (flexural or shear) nominally tested in the studies aren't always achieved
20 in the experiment and criteria must be applied to determine the failure type. This can be
21 done using Model Code 2010 provisions and comparing the difference between the test-
22 to-predicted shear and flexural strength ratios. Using these criteria, out of 194 results, 49
23 were identified as flexural failure, 69 as shear failure without stirrups and 25 as shear
24 failure with stirrups while for 51 results the failure type could not be clearly identified.
- 25 3. Eurocode 2 predictions of flexural strength are accurate and precise with a mean value of
26 test-to-predicted strength ratio of 1.064 for NAC, 1.079 for RAC50, and 1.091 for RAC100
27 beams. The CoVs are 8.64%, 14.36%, and 13.24% respectively. Using the statistical *t*-test
28 it was shown that these three samples show no significant difference between them.

1 Flexural strength of RAC beams can be calculated using the existing provisions without
2 any alterations.

- 3 4. Eurocode 2 predictions of shear strength for beams without stirrups are accurate but less
4 precise compared to flexural strength. The mean value of test-to-predicted strength ratio is
5 1.030 for NAC, 1.060 for RAC50, and 1.054 for RAC100 beams while the CoVs are
6 27.03%, 14.25%, and 22.07% respectively. Using the statistical *t*-test it was shown that
7 these three samples show no significant difference between them. Shear strength of RAC
8 beams without stirrups can be calculated using the existing provisions without any
9 alterations.
- 10 5. Eurocode 2 predictions of shear strength for beams with stirrups are both inaccurate and
11 imprecise. The mean value of test-to-predicted strength ratio is 1.346 for NAC, 1.861 for
12 RAC50, and 1.682 for RAC100 beams while the CoVs are 25.03%, 15.34%, and 20.71%
13 respectively. Using the statistical *t*-test it was shown that these three samples are
14 significantly different. This was because most of the experiments on RAC beams were
15 carried out applying close to minimum transverse reinforcement ratios and for this type of
16 beams Eurocode 2 predictions are equally inaccurate and imprecise for both RAC and
17 NAC beams. The difference between NAC and RAC beams arose only when other results
18 on NAC beams from literature were added, with high transverse reinforcement ratios. More
19 experiments on RAC beams with larger than minimum transverse reinforcement ratios
20 should be carried out in order to draw a final conclusion.
- 21 6. A sensitivity analysis by selection criteria variation showed that the database of flexural
22 strength is insensitive to criteria variation whereas the databases of shear strengths with
23 and without stirrups are somewhat sensitive. For beams without stirrups this can be
24 explained by a large scatter of the test-to-predicted strength ratio whereas for beams with
25 stirrups the reason is the small number of results on RAC beams.

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3 **Appendix A. Supplementary data**

4 Supplementary data associated with this article can be found in the online version.

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- 15 | Figure [1115](#). Model factor for Eurocode 2 predictions of shear strength for beams with stirrups
16 | compared to shear span-to-effective depth ratio

Table 1. Eurocode 2 predictions of flexural strength for 49 selected beams

Study	Specimen	RCA (%)	b_w (mm)	d (mm)	ρ_l (%)	f_{yl} (MPa)	f_c (MPa)	$M_{E,test}$ (kNm)	$M_{R,pred}$ (kNm)	γ_{II}
[27]	V45-03-WB	0	150	160	1.06	331	57.0	15.0	13.6	1.10
	VEX45-03-WB		150	160	1.06	331	55.3	15.3	13.6	1.13
	V-01-10WB		150	160	0.59	331	30.6	8.0	8.0	1.00
	V-01-10DB		150	160	0.59	331	32.5	9.1	8.0	1.13
[30]	CL-Av		200	304	1.99	420	37.1	142.7	165.1	0.86
	CG-Av		200	304	1.99	420	33.8	139.1	162.4	0.86
[34]	BSF4-A0		400	525	2.34	380	26.9	878.9	813.8	1.08
[35]	NAC1a		200	268	0.28	640	35.0	28.4	25.2	1.13
	NAC2a		200	263	1.46	550	35.0	108.6	97.5	1.11
	NAC3a		200	244	2.54	550	35.0	137.6	134.8	1.02
[38]	F0-1a		150	200	1.3	572	38.6	42.6	41.3	1.03
	F0-1b		150	200	1.3	572	38.6	43.1	41.3	1.04
	F0-2a		150	200	1.3	572	46.5	43.8	42.1	1.04
	F0-2b		150	200	1.3	572	46.5	43.8	42.1	1.04
[39]	N0-0.5		135	230	0.5	377	38.6	15.9	13.3	1.20
	N0-1.0		135	230	1	408	38.6	28.2	23.8	1.19
	N0-1.5		135	230	1.5	389	38.6	36.9	33.6	1.10
	N0-1.8		135	230	1.8	410	38.6	52.8	48.1	1.10
[35]	RAC50-1a	50	200	268	0.28	640	35.4	27.0	25.2	1.07
	RAC50-2a		200	263	1.46	550	35.4	110.6	97.6	1.13
	RAC50-3a		200	244	2.54	550	35.4	160.4	135.2	1.19
[38]	F50-1a		150	200	1.3	572	40.0	41.8	41.5	1.01
	F50-1b		150	200	1.3	572	40.0	43.1	41.5	1.04
	F50-2a		150	200	1.3	572	39.3	41.3	41.4	1.00
	F50-2b		150	200	1.3	572	39.3	41.3	41.4	1.00
[39]	N50-0.5		135	230	0.5	377	29.0	13.6	13.2	1.03
	N50-1.0		135	230	1	408	29.0	24.4	23.4	1.04
	N50-1.5		135	230	1.5	389	29.0	32.8	32.8	1.00
	N50-1.8		135	230	1.8	410	29.0	50.5	46.4	1.09
[30]	EM-Min	63.5	200	304	0.49	420	41.6	46.0	29.5	1.56
	EM-Av		200	304	1.99	420	41.6	149.2	168.1	0.89
	EM-Max		200	304	3.26	420	41.6	221.9	208.7	1.06
[30]	EV-Min	74.3	200	304	0.49	420	49.1	46.7	29.6	1.58
	EV-Av		200	304	1.99	420	49.1	150.2	171.9	0.87
	EV-Max		200	304	3.26	420	49.1	225.2	215.1	1.05
[27]	CR45-03-WB	100	150	160	1.06	331	46.5	14.8	13.5	1.10
	CREX45-03-WB		150	160	1.06	331	46.6	15.1	13.5	1.12
	CR45-01-10WB		150	160	0.59	331	30.4	8.5	8.0	1.06
	CR45-01-10DB		150	160	0.59	331	28.4	8.9	8.0	1.11
	CR60-01-10WB		150	160	0.59	331	34.5	9.3	8.1	1.16
	CR60-01-10DB		150	160	0.59	331	31.8	9.5	8.0	1.18
[34]	BSF4-A100		400	525	2.34	380	26.9	817.6	813.8	1.00
[35]	RAC100-1a		200	268	0.28	640	34.0	26.8	25.2	1.07
	RAC100-2a		200	263	1.46	550	34.0	105.4	97.1	1.09
	RAC100-3a		200	244	2.54	550	34.0	142.6	133.7	1.07
[38]	F100-1a		150	200	1.3	572	43.8	41.7	41.9	1.00
	F100-1b		150	200	1.3	572	43.8	41.7	41.9	1.00
	F100-2a		150	200	1.3	572	38.5	44.1	41.3	1.07
	F100-2b		150	200	1.3	572	38.5	42.5	41.3	1.03

Table 2. Statistical descriptors of model factors for Eurocode 2 predictions of beams' flexural strength

Concrete	Sample size, n	Mean, μ	Standard deviation, σ	CoV (%)	<u>Results outside the 5-95% range</u>
NAC	18	1.064	0.092	8.64	<u>2</u>
RAC50	14	1.079	0.155	14.36	<u>2</u>
RAC100	17	1.091	0.144	13.24	<u>2</u>

Table 3. Eurocode 2 predictions of shear strength for 69 selected beams without stirrups

Study	Specimen	RCA (%)	b_w (mm)	d (mm)	a/d	ρ_l (%)	f_c (MPa)	$V_{E,test}$ (kN)	$V_{R,pred}$ (kN)	γ_{sh}
[26]	HC-1	0	200	303	3.3	2.98	41.9	100.5	86.5	1.16
[28]	V0CC		200	303	3.3	2.98	40.2	88.9	85.3	1.04
[31]	CL-M		200	309	2.6	1.62	38.8	92.8	79.8	1.16
	CG-2.7		200	309	2.6	1.62	34.4	150.0	76.7	1.96
[32]	NANAC-H2.5		200	360	2.5	1.61	24.7	90.7	77.2	1.17
	NANAC-H3.25		200	360	3.25	1.61	24.7	71.1	77.2	0.92
	NANAC-L2.5		200	360	2.5	0.53	24.7	66.2	53.3	1.24
	NANAC-M2.5		200	360	2.5	0.83	24.7	72.0	61.9	1.16
[36]	NAC1b		200	235	4.2	4.09	30.8	106.3	64.2	1.65
[37]	NA-S2		200	300	2.5	1.94	31.8	75.5	77.5	0.97
	NA-M2		200	450	2.5	1.93	31.8	106.9	106.4	1.00
	NA-L2		200	600	2.5	1.94	31.8	125.9	134.5	0.94
	NA-M3		300	450	2.5	2.00	31.8	156.7	161.5	0.97
	NA-L4		400	600	2.5	1.94	31.8	256.4	269.0	0.95
[40]	NAC NS-6 1		300	375	3.2	2.03	37.3	143.2	147.5	0.97
	NAC NS-8 1		300	375	3.2	2.71	37.3	173.5	147.5	1.18
	NAC NS-4 2		300	400	3	1.27	34.2	129.9	129.6	1.00
	NAC NS-6 2		300	375	3.2	2.03	34.2	167.0	143.3	1.17
	NAC NS-8 2		300	375	3.2	2.71	34.2	170.8	143.3	1.19
[38]	S0-1a		150	200	3.8	1.30	32.6	31.1	37.7	0.83
	S0-1b		150	200	3.8	1.30	32.6	36.9	37.7	0.98
	S0-2a		150	200	3.8	1.30	50.3	40.4	43.5	0.93
	S0-2b		150	200	3.8	1.30	50.3	42.3	43.5	0.97
[26]	HR50-1	50	200	303	3.3	2.98	41.3	89.0	86.1	1.03
[28]	V0RC		200	303	3.3	2.98	39.7	90.6	85.0	1.07
[32]	RARAC50-H2.5		200	360	2.5	1.61	24.1	87.9	76.6	1.15
	RARAC50-H3.25		200	360	3.25	1.61	24.1	71.6	76.6	0.93
	RARAC50-M2.5		200	360	2.5	0.83	24.1	67.1	61.4	1.09
[36]	RAC50-1b		200	235	4.2	4.09	33.4	91.8	66.0	1.39
[37]	RH-S2		200	300	2.5	1.94	32.6	60.6	78.1	0.78
	RH-M2		200	450	2.5	1.93	32.6	108.9	107.3	1.01
	RH-L2		200	600	2.5	1.94	32.6	126.1	135.6	0.93
	RH-M3		300	450	2.5	2.00	32.6	154.2	162.9	0.95
	RH-L4		400	600	2.5	1.94	32.6	261.5	271.3	0.96
[40]	RAC50 NS-6 1		300	375	3.2	2.03	32.1	151.3	140.3	1.08
	RAC50 NS-8 1		300	375	3.2	2.71	32.1	171.8	140.3	1.22
	RAC50 NS-6 2		300	375	3.2	2.03	35.5	148.6	145.1	1.02
	RAC50 NS-8 2		300	375	3.2	2.71	35.5	168.7	145.1	1.16
[38]	S50-1a		150	200	3.8	1.30	43.6	44.0	41.5	1.06
	S50-1b		150	200	3.8	1.30	43.6	39.1	41.5	0.94
	S50-2a		150	200	3.8	1.30	40.2	43.7	40.4	1.08
	S50-2b		150	200	3.8	1.30	40.2	41.2	40.4	1.02
[33]	EM-4	63.5	200	305	3.9	2.46	41.6	83.2	86.7	0.96
	EM-L		200	201	2.7	1.99	41.6	89.3	63.0	1.42
	EM-2.7		200	309	2.6	1.62	41.6	103.9	81.7	1.27
	EM-H		200	381	2.7	1.83	41.6	99.5	100.2	0.99
	EM-VH		200	476	2.7	1.68	41.6	104.6	116.3	0.90
[33]	EV-4	74.3	200	305	3.9	2.46	49.1	105.6	91.7	1.15
	EV-L		200	201	2.6	1.99	49.1	122.6	66.6	1.84
	EV-H		200	381	2.7	1.83	49.1	111.7	105.9	1.05
	EV-VH		200	476	2.7	1.68	49.1	119.6	122.9	0.97
[25]	R3.0-N	100	170	270	3	1.10	31.2	55.1	50.0	1.10
[26]	HR100-1		200	303	3.3	2.98	39.8	84.0	85.0	0.99
[32]	RARAC100-H2.5		200	360	2.5	1.61	22.6	84.8	75.0	1.13
	RAC100-M2.5		200	360	2.5	0.83	22.6	70.1	60.1	1.17
[36]	RAC1000-1b		200	235	4.2	4.09	34.5	104.8	66.7	1.57
[37]	RF-S2		200	300	2.5	1.94	34.9	72.9	79.9	0.91
	RF-M2		200	450	2.5	1.93	34.9	96.4	109.8	0.88
	RF-L2		200	600	2.5	1.94	34.9	125.1	138.8	0.90

	RF-M3	300	450	2.5	2.00	34.9	159.8	166.6	0.96
	RF-L4	400	600	2.5	1.94	34.9	256.6	277.5	0.92
[40]	RAC100 NS-6 1	300	375	3.2	2.03	30.0	143.2	137.2	1.04
	RAC100 NS-8 1	300	375	3.2	2.71	30.0	131.4	137.2	0.96
	RAC100 NS-6 2	300	375	3.2	2.03	34.1	124.1	143.2	0.87
	RAC100 NS-8 2	300	375	3.2	2.71	34.1	140.3	143.2	0.98
[38]	S100-1a	150	200	3.8	1.30	41.4	36.4	40.8	0.89
	S100-1b	150	200	3.8	1.30	41.4	38.0	40.8	0.93
	S100-2a	150	200	3.8	1.30	35.7	39.9	38.8	1.03
	S100-2b	150	200	3.8	1.30	35.7	36.1	38.8	0.93

Table 4. Statistical descriptors of model factors for Eurocode 2 predictions of shear strength for beams without stirrups

Concrete	Sample size, n	Mean, μ	Standard deviation, σ	CoV (%)	<u>Results outside the 5-95% range</u>
NAC	530	1.030	0.279	27.03	<u>75</u>
RAC50	24	1.060	0.151	14.25	<u>0</u>
RAC100	22	1.054	0.233	22.07	<u>2</u>

Table 5. Eurocode 2 predictions of shear strength for [25](#) selected beams with stirrups

Study	Specimen	RCA (%)	b_w (mm)	d (mm)	a/d	A_{sw} (mm ²)	s (mm)	f_{yw} (mm ²)	θ (°)	$V_{E,test}$ (kN)	$V_{R,pred}$ (kN)	γ_{sh}
[26]	HC-2	0	200	303	3.3	57	130	544	19	213.0	161.3	1.32
	HC-3		200	303	3.3	57	170	544	30	177.0	86.5	2.05
	HC-4		200	303	3.3	57	240	544	28	187.5	86.5	2.17
[28]	V24CC		200	303	3.3	57	240	500	22	128.0	84.6	1.51
	V17CC		200	303	3.3	57	170	500	24	150.8	101.9	1.48
	V13CC		200	303	3.3	57	130	500	26	190.3	121.6	1.56
[29]	BNN-lb2		200	250	3.2	57	100	234	30	115.5	68.0	1.70
[36]	NAC3b		200	235	4.2	57	150	300	21	159.9	64.2	2.49
[26]	HR50-2	50	200	303	3.3	57	130	544	28	220.0	121.4	1.81
	HR50-3		200	303	3.3	57	170	544	22	176.0	122.1	1.44
	HR50-4		200	303	3.3	57	240	544	21	164.0	87.4	1.88
[28]	V24RC		200	303	3.3	57	240	500	25	164.3	84.7	1.94
	V17RC		200	303	3.3	57	170	500	35	177.0	86.2	2.05
	V13RC		200	303	3.3	57	130	500	21	233.6	148.3	1.58
[36]	RAC50-3b		200	235	4.2	57	150	300	21	156.9	66.0	2.38
[31]	EM-6S-D		63.5	200	301	2.7	157	200	530	31	341.0	187.7
[31]	EV-3S-R	74.3	200	301	2.7	101	200	530	27	235.0	141.6	1.66
	EV-6S-D		200	301	2.7	157	200	530	28	327.0	212.1	1.54
[26]	HR100-2	100	200	303	3.3	57	130	544	22	189.5	159.7	1.19
	HR100-3		200	303	3.3	57	170	544	24	163.0	110.8	1.47
	HR100-4		200	303	3.3	101	240	544	29	168.0	112.6	1.49
[29]	ORN-lb2		200	250	3.2	57	100	234	26	118.0	66.2	1.78
	BRN-lb2		200	250	3.2	57	100	234	26	120.5	65.7	1.83
	GRN-lb2		200	250	3.2	57	100	234	26	116.5	67.8	1.72
[36]	RAC100-3b		200	235	4.2	57	150	300	21	163.4	66.7	2.45

Table 6. Statistical descriptors of model factors for Eurocode 2 predictions of shear strength for beams with stirrups

Concrete	Sample size, n	Mean, μ	Standard deviation, σ	CoV (%)	<u>Results outside the 5–95% range</u>
NAC	45	1.346	0.337	25.03	<u>4</u>
RAC50	8	1.861	0.286	15.34	<u>3</u>
RAC100	9	1.682	0.348	20.71	<u>1</u>

Table 7[Click here to download Table: Table_7.docx](#)

Table 7. Statistical descriptors of model factors for Eurocode 2 predictions of beam's flexural and shear strength for different database selection criteria

Database	Concrete	n	$\Delta_{cr} = 0.25$		$\Delta_{cr} = 0.45$		
			μ	CoV (%)	n	μ	CoV (%)
Flexure	NAC	23	1.070	7.95	14	1.086	5.63
	RAC50	14	1.079	14.36	14	1.079	14.36
	RAC100	23	1.090	11.50	15	1.088	14.17
Shear NS	NAC	595	1.117	25.50	429	1.177	26.32
	RAC50	27	1.048	14.29	21	1.079	13.25
	RAC100	27	1.034	21.35	18	1.075	23.20
Shear S	NAC	50	1.348	24.67	38	1.375	25.23
	RAC50	8	1.861	15.34	7	1.868	16.49
	RAC100	12	1.683	18.72	3	1.966	24.91

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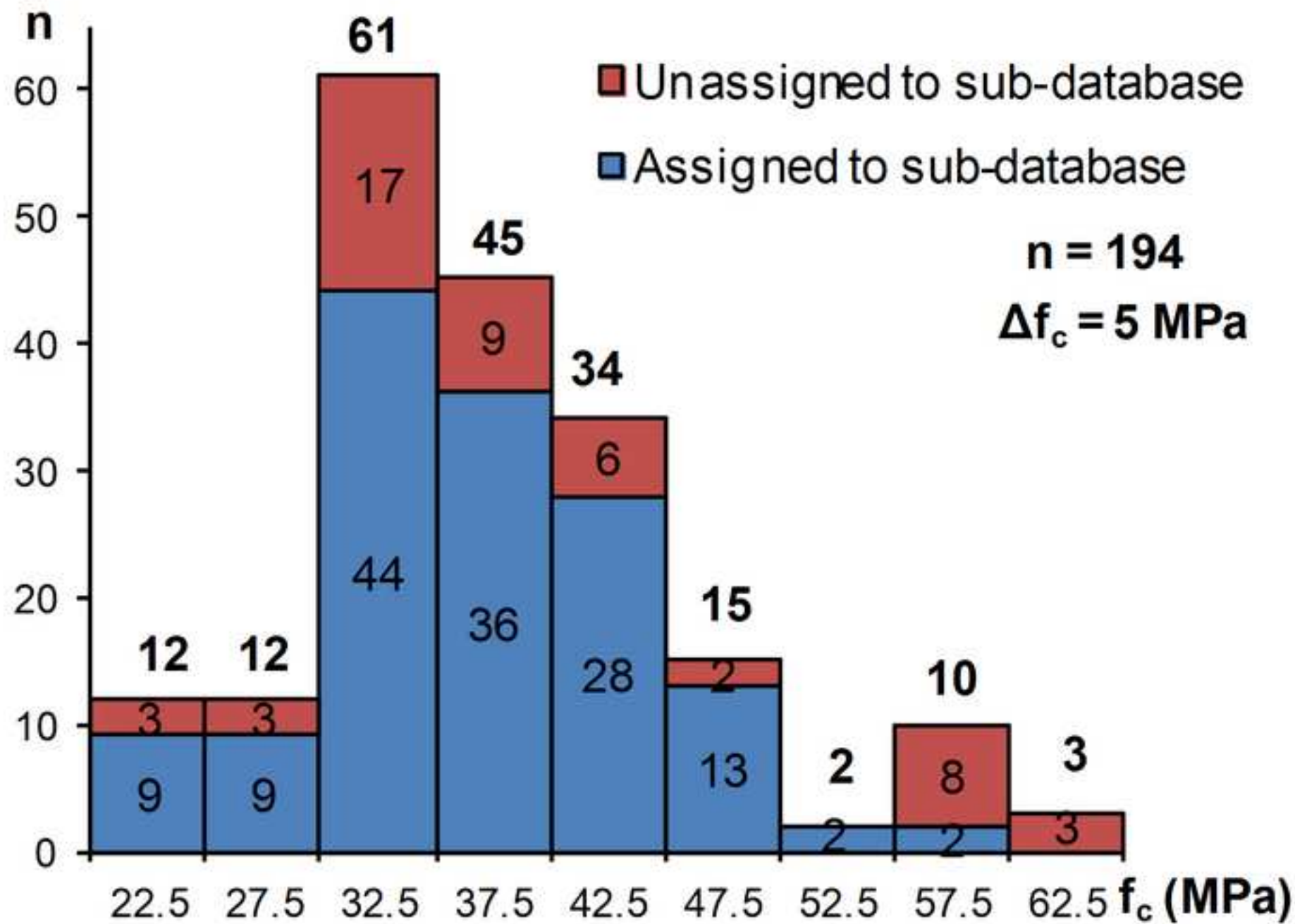


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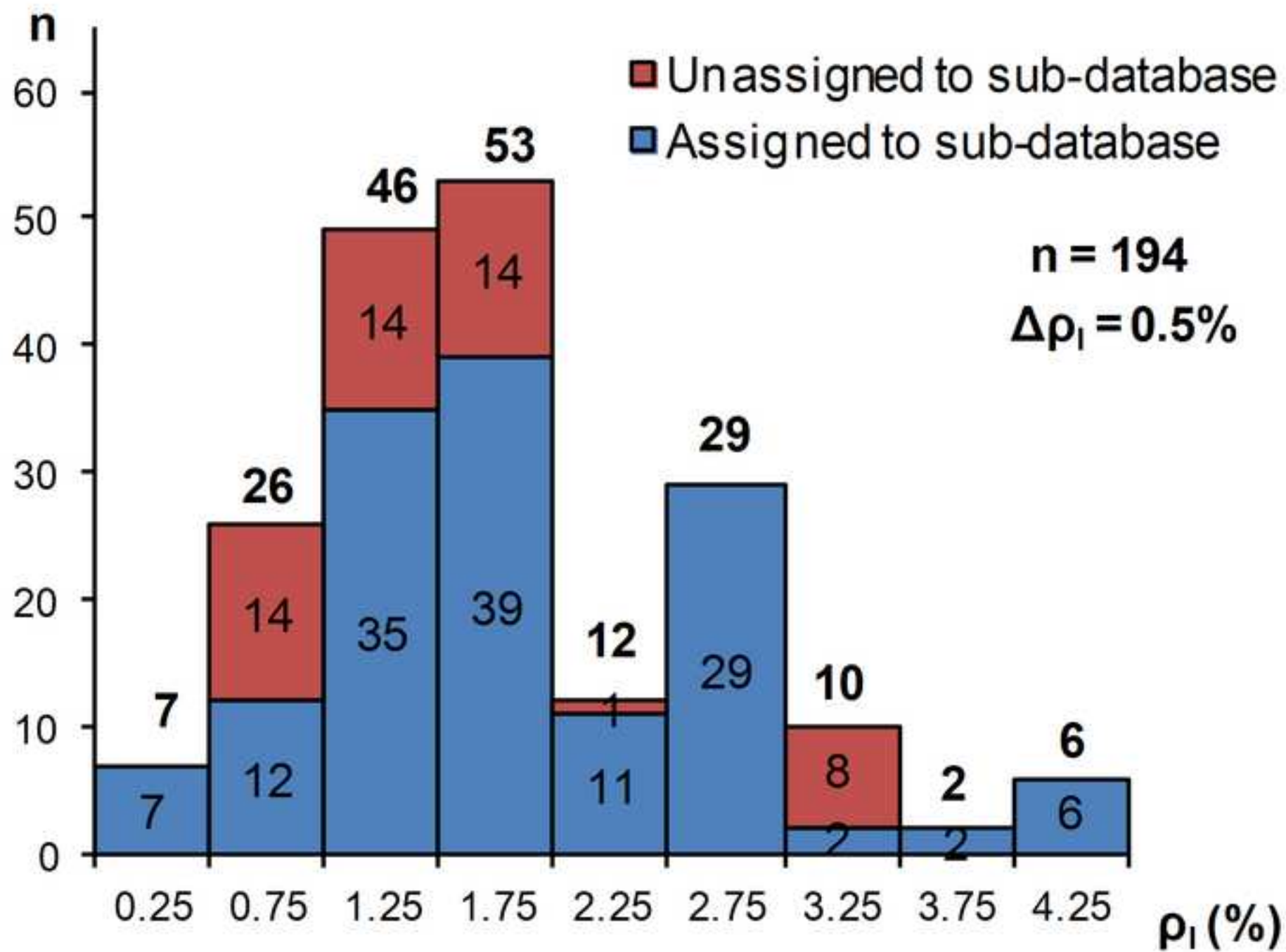


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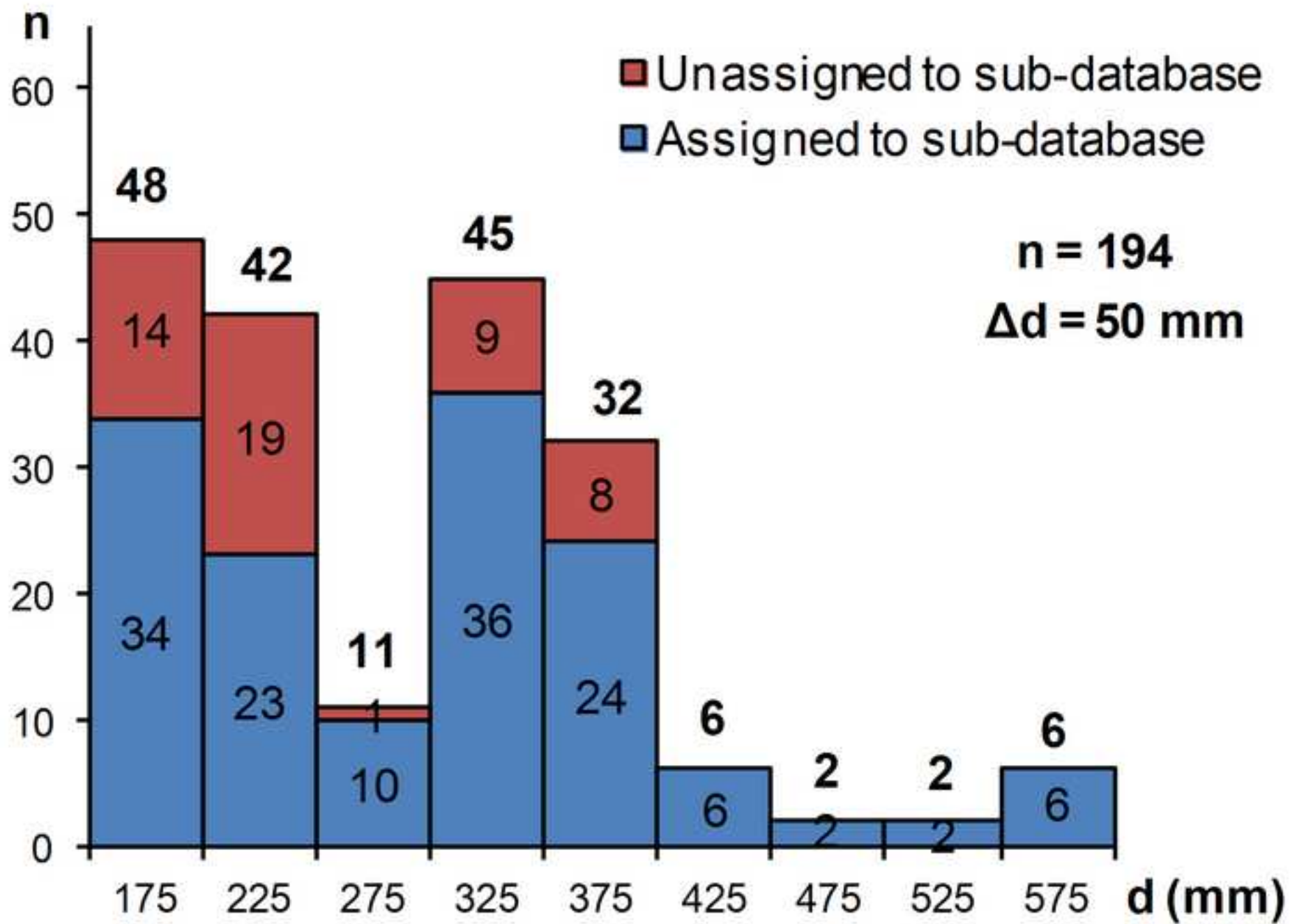


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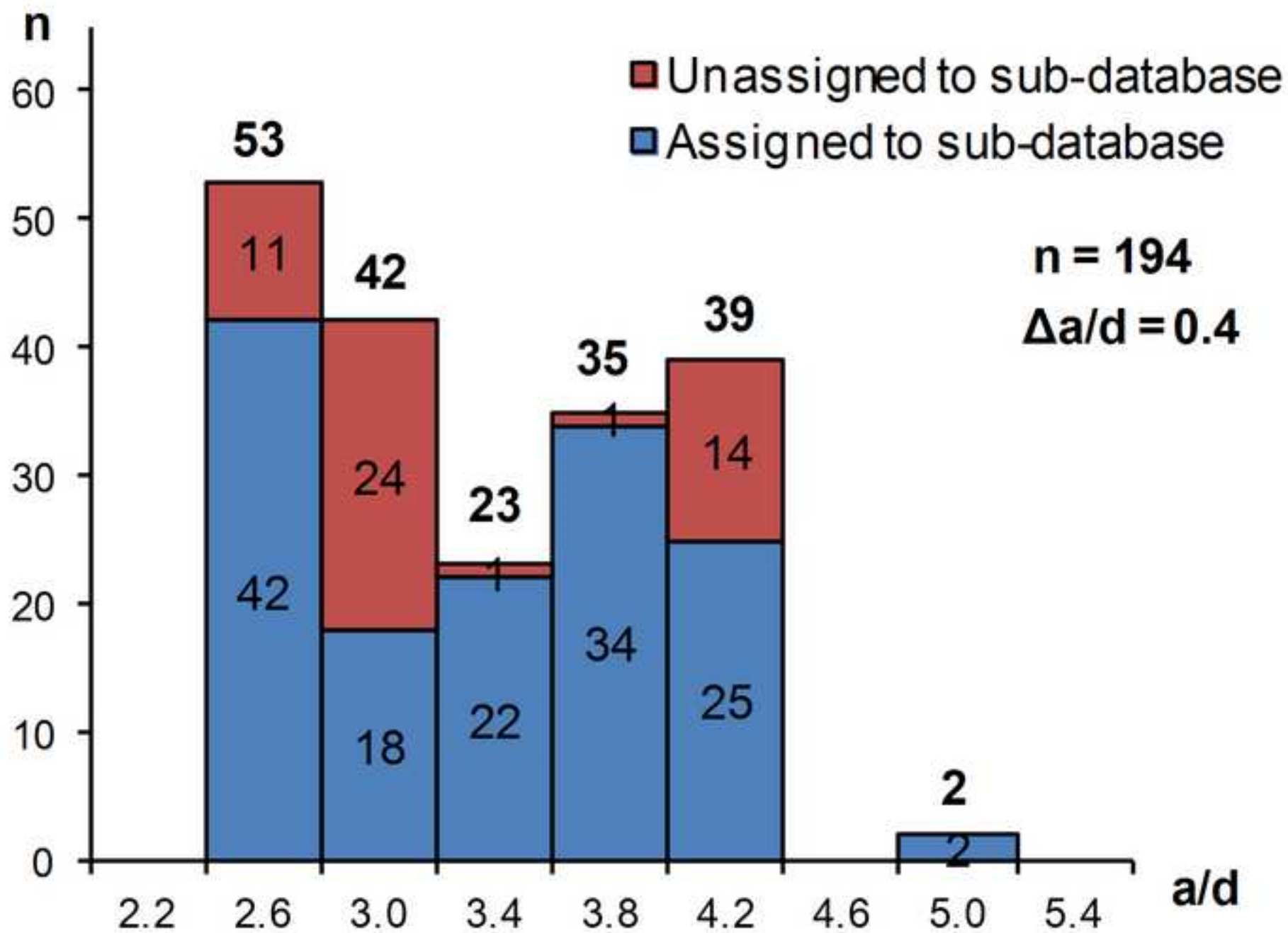


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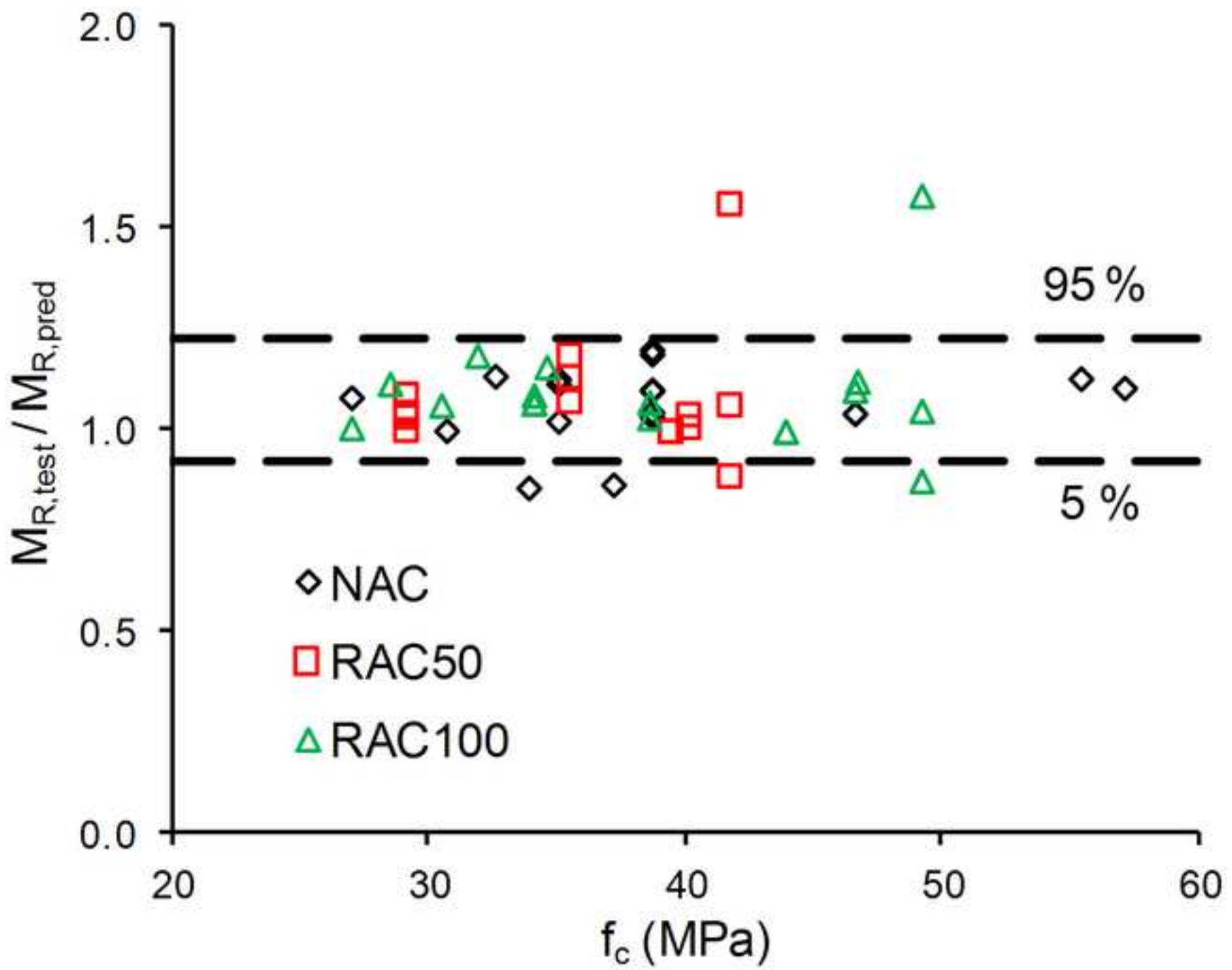


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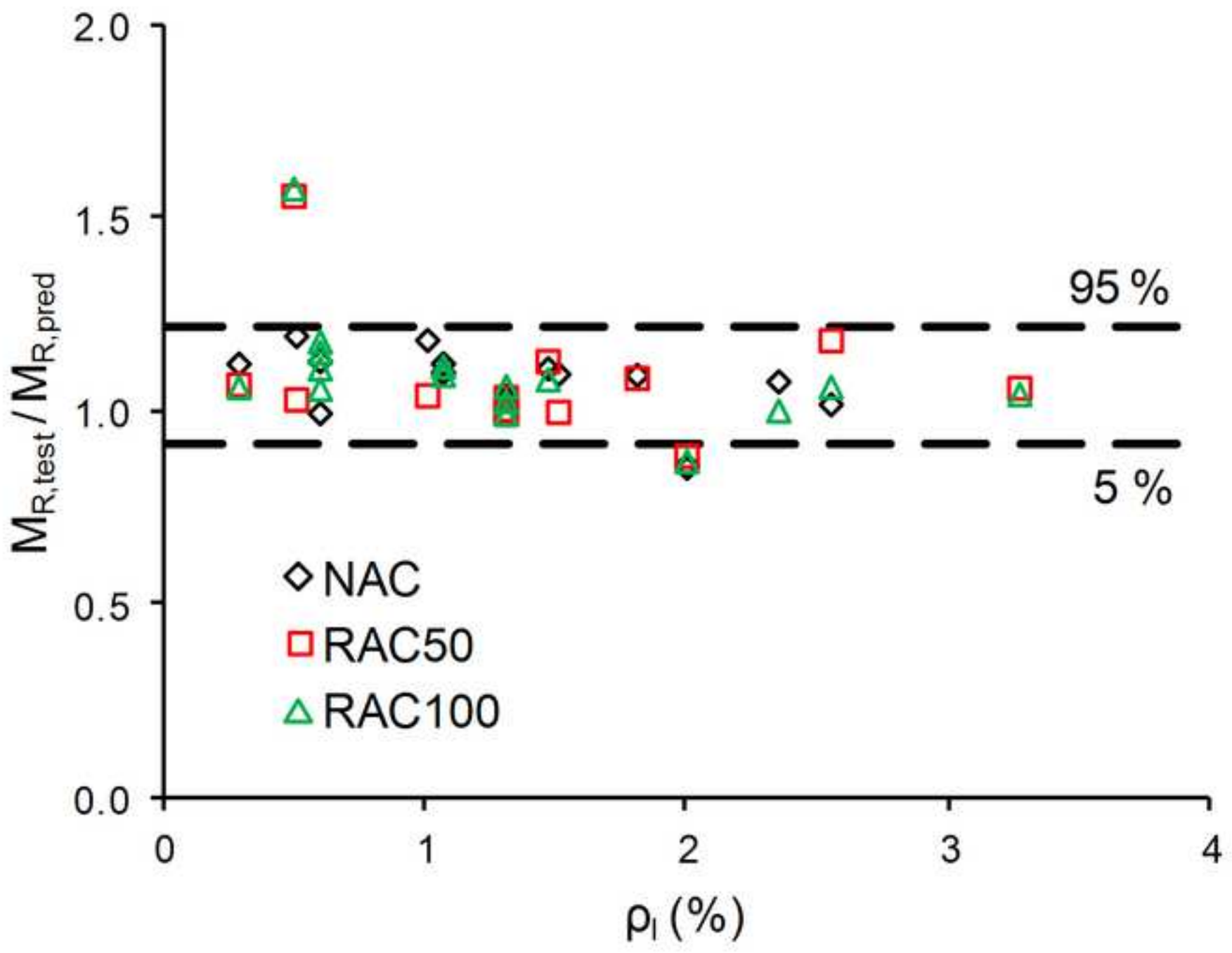


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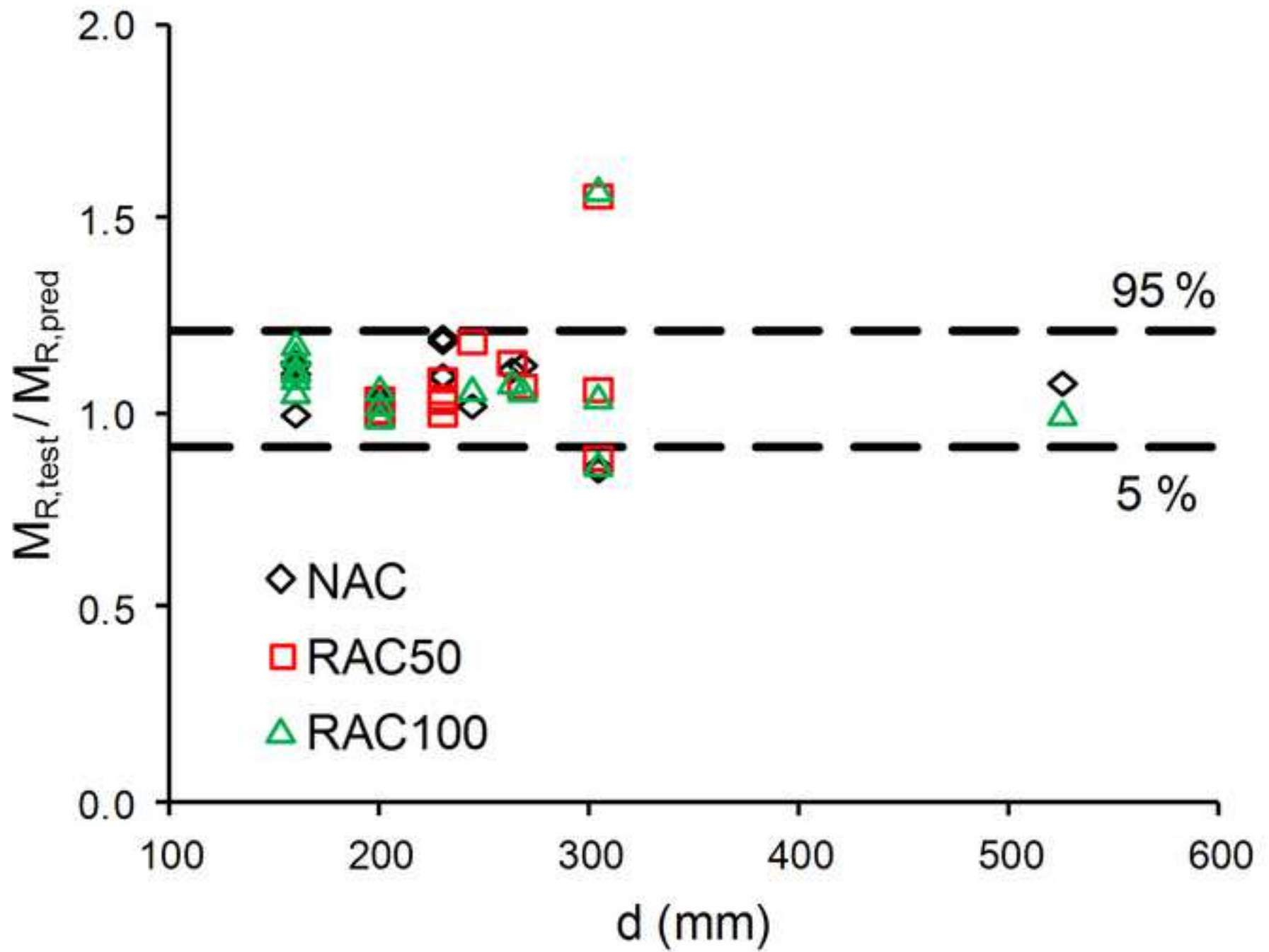


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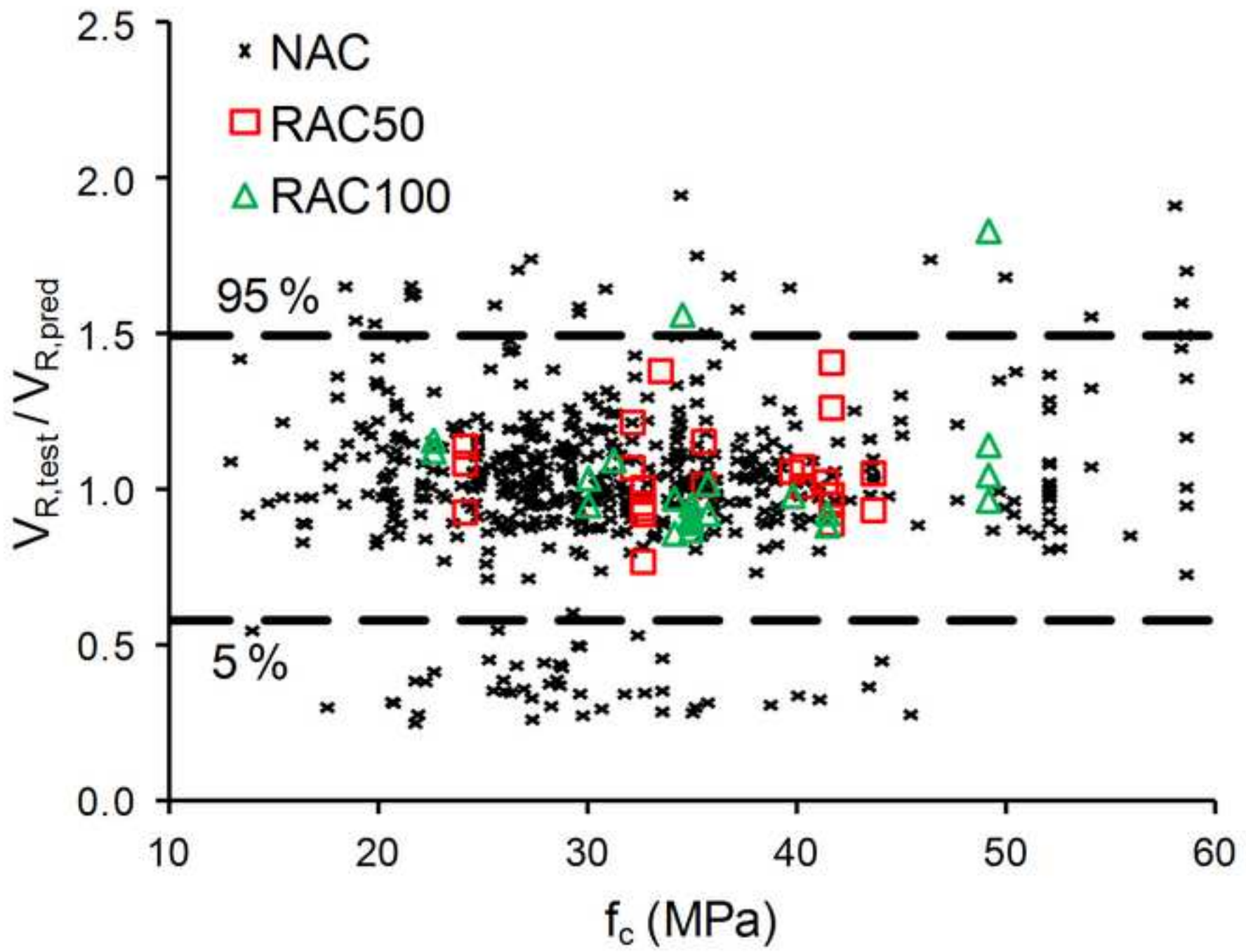


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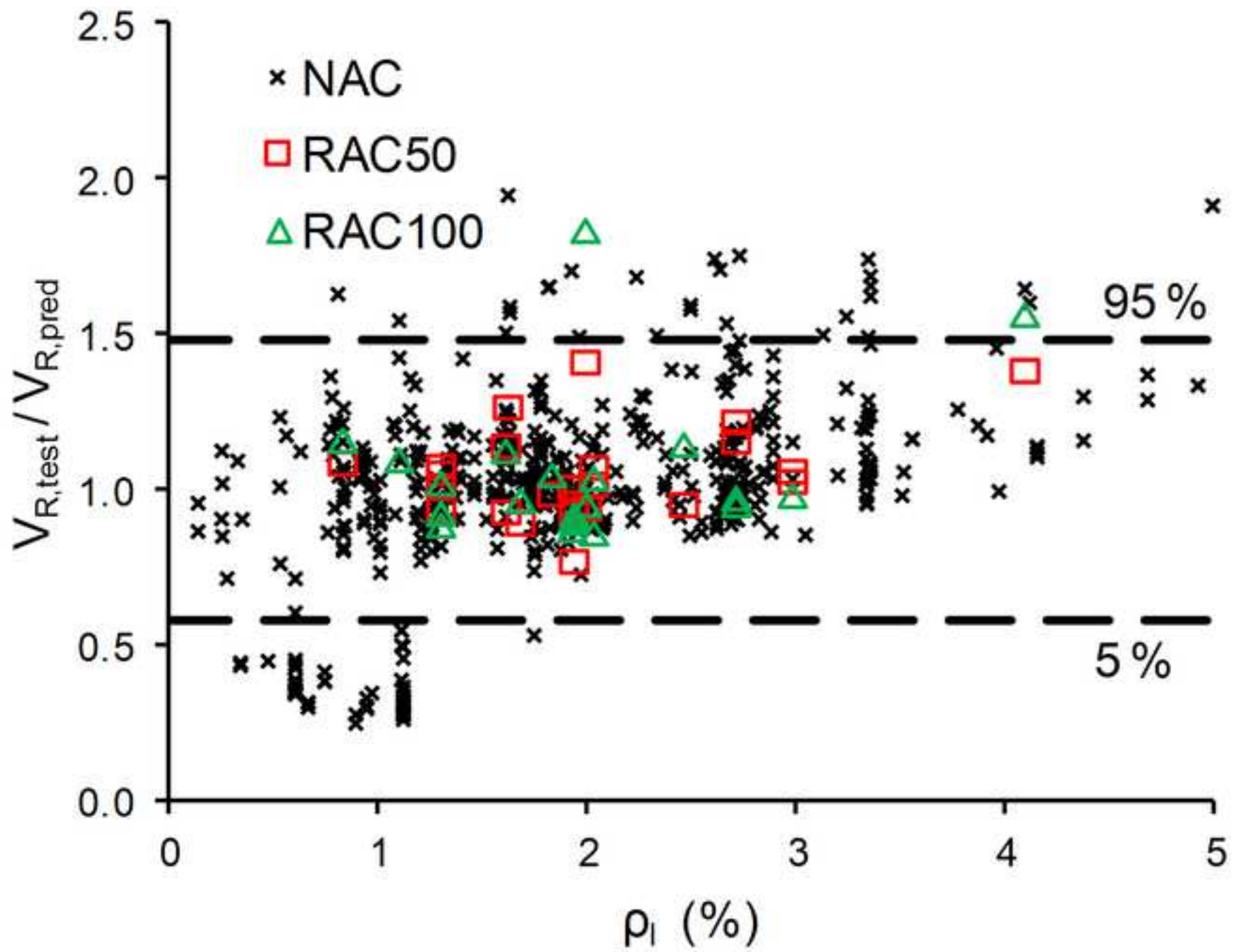


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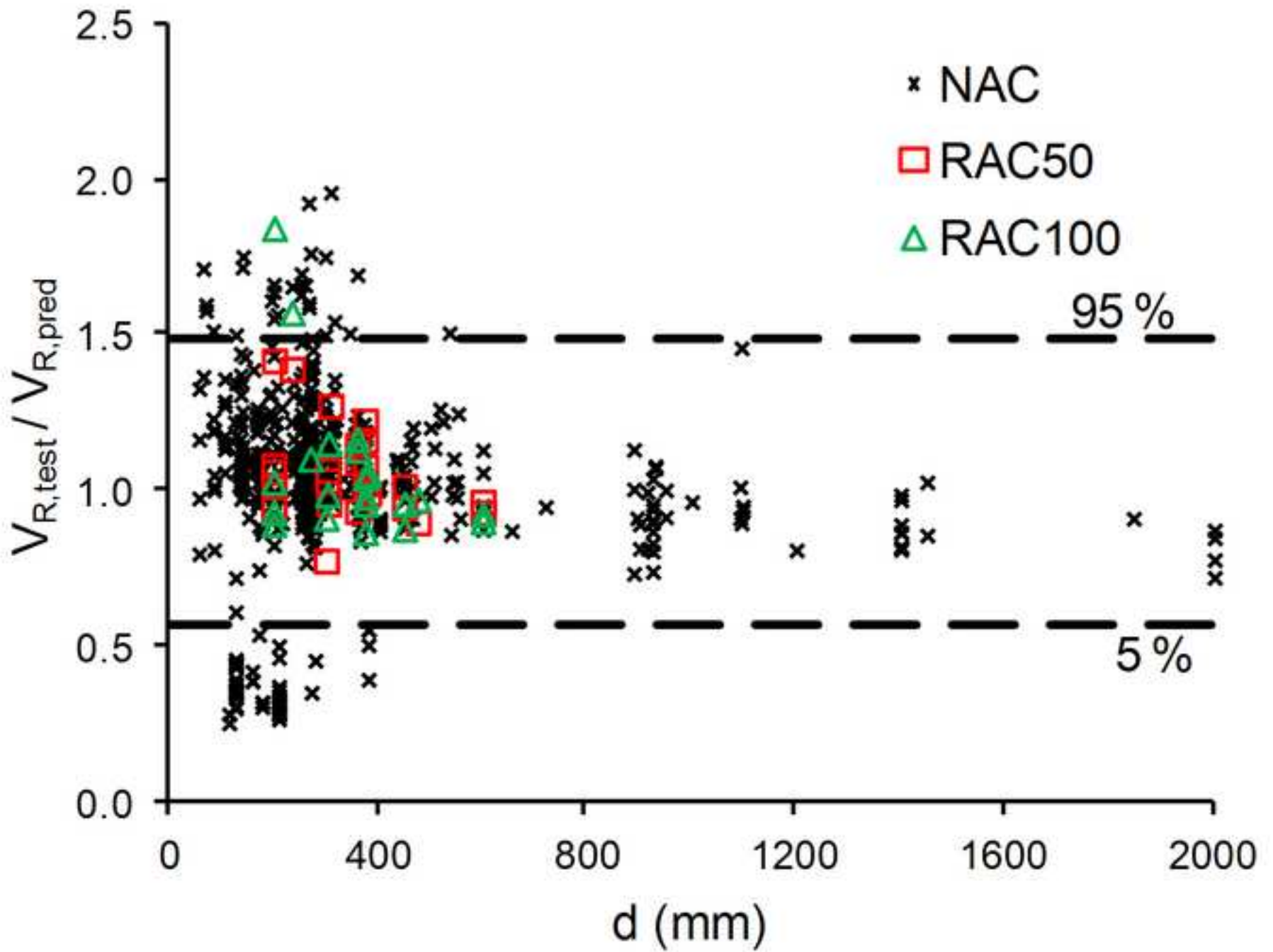


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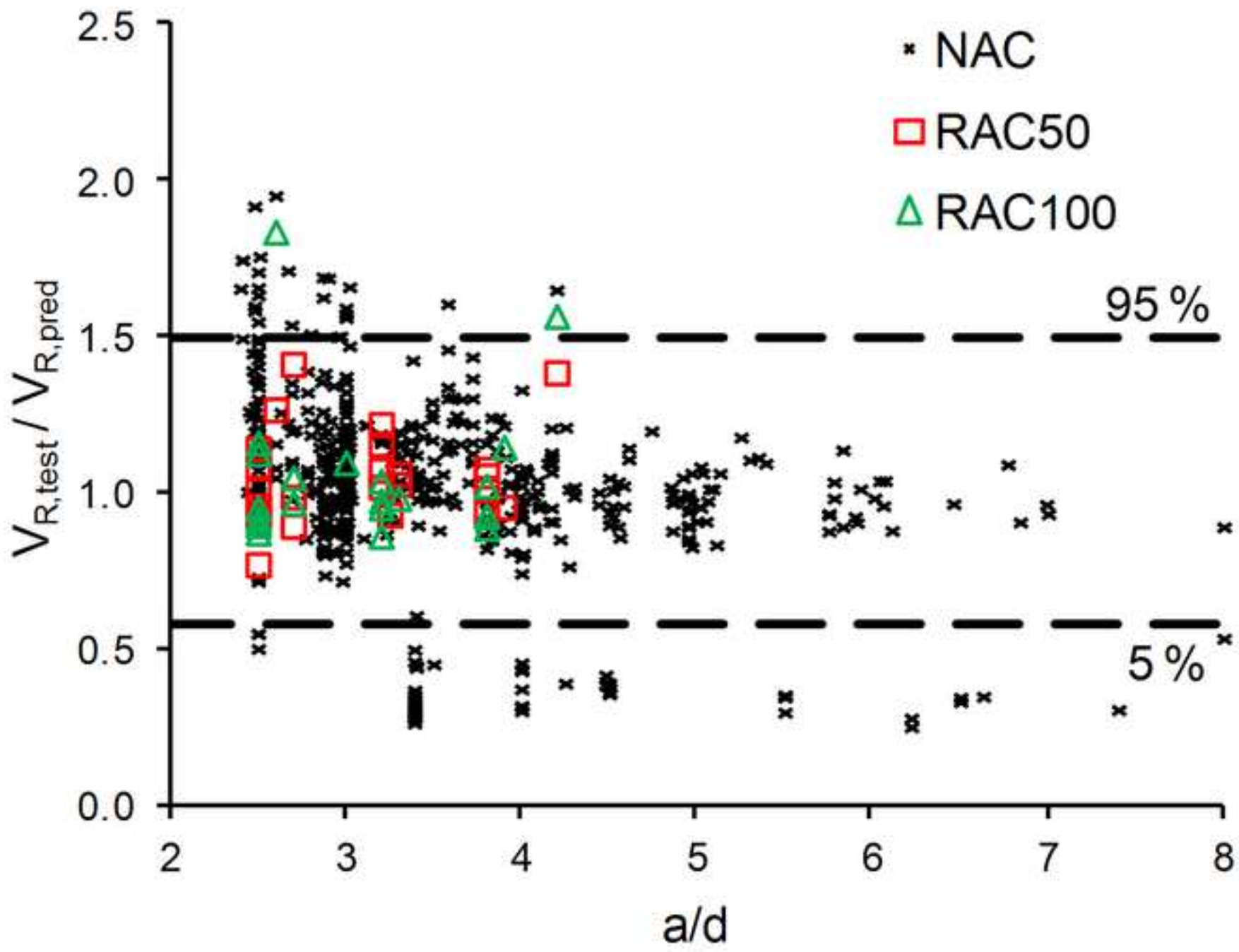


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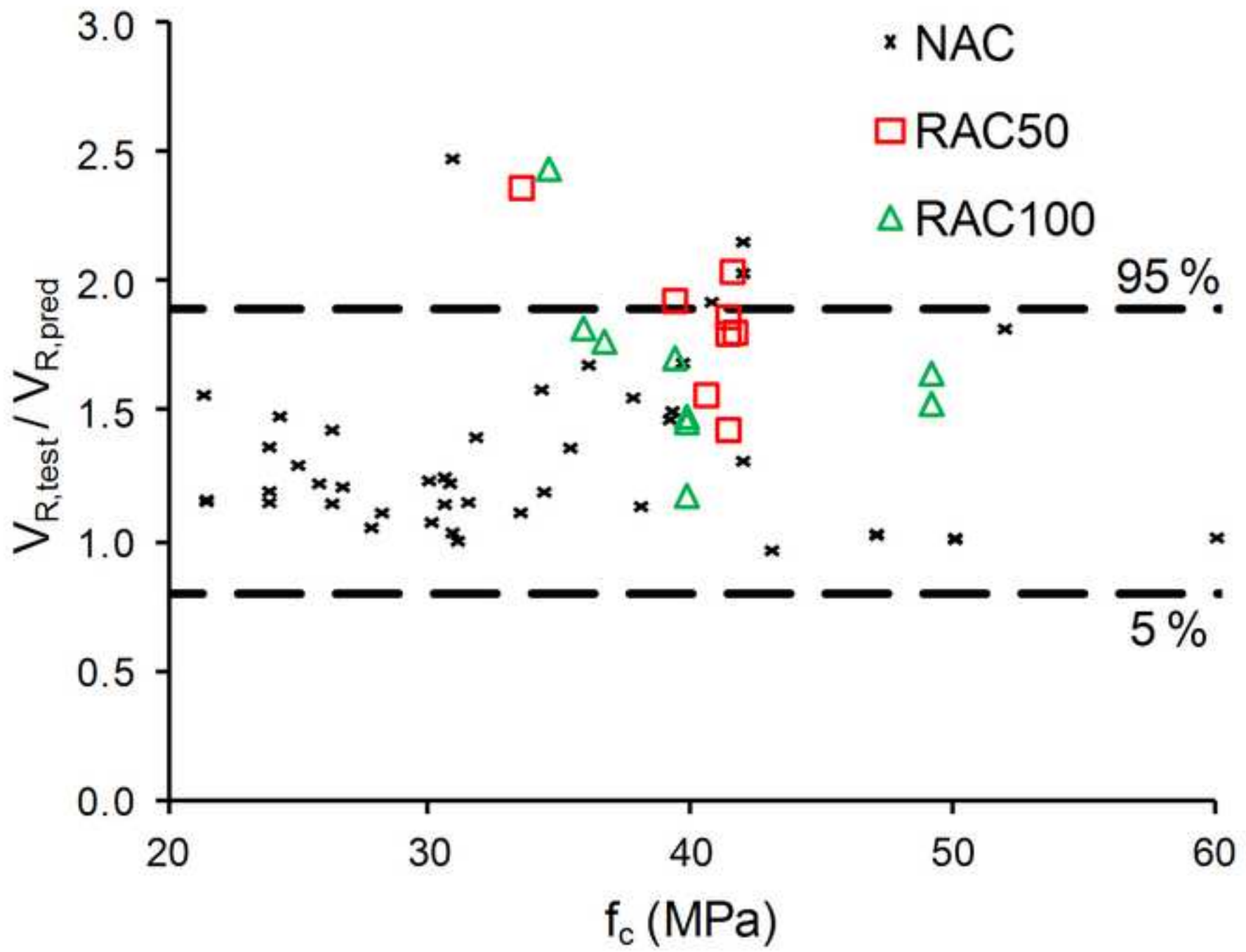


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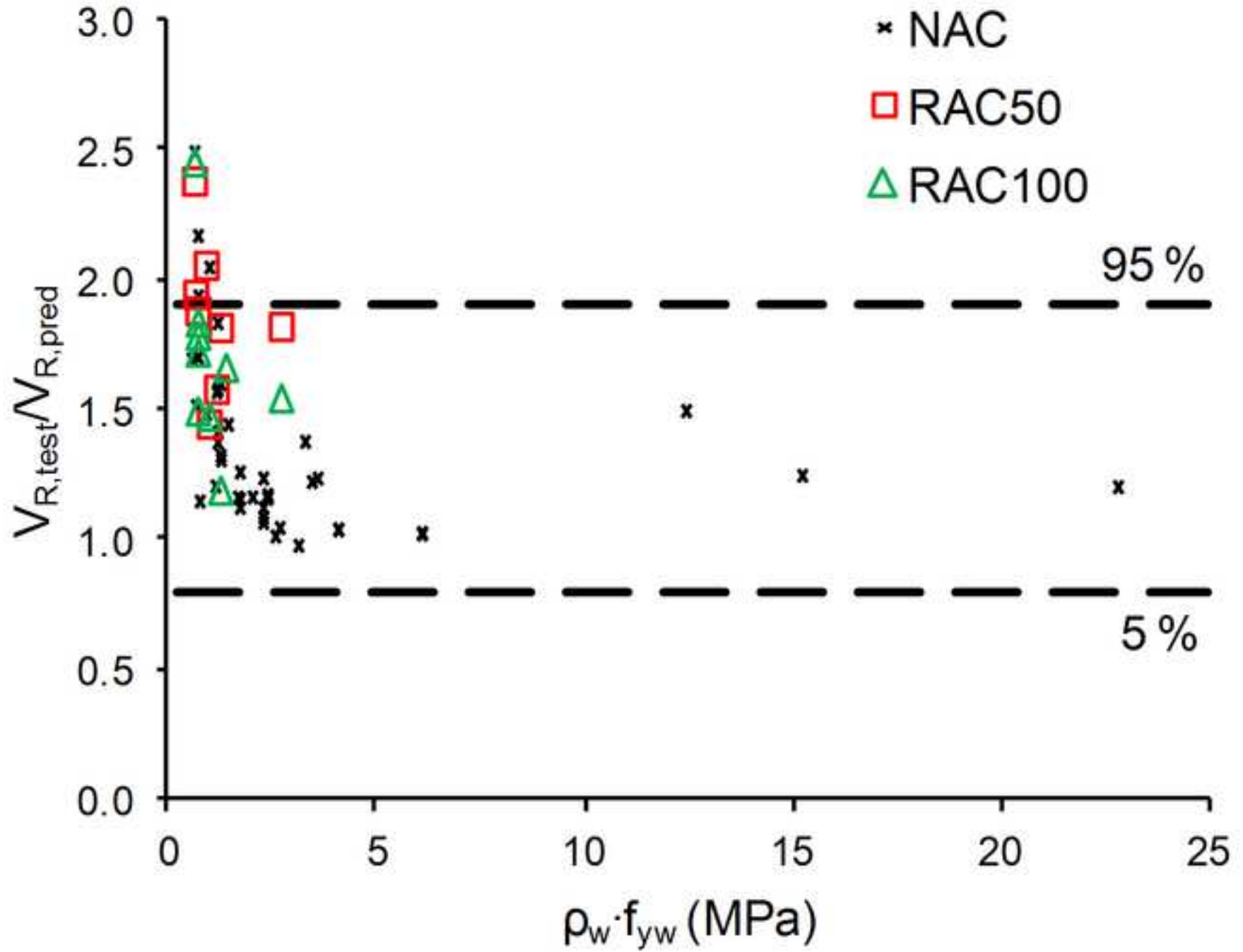


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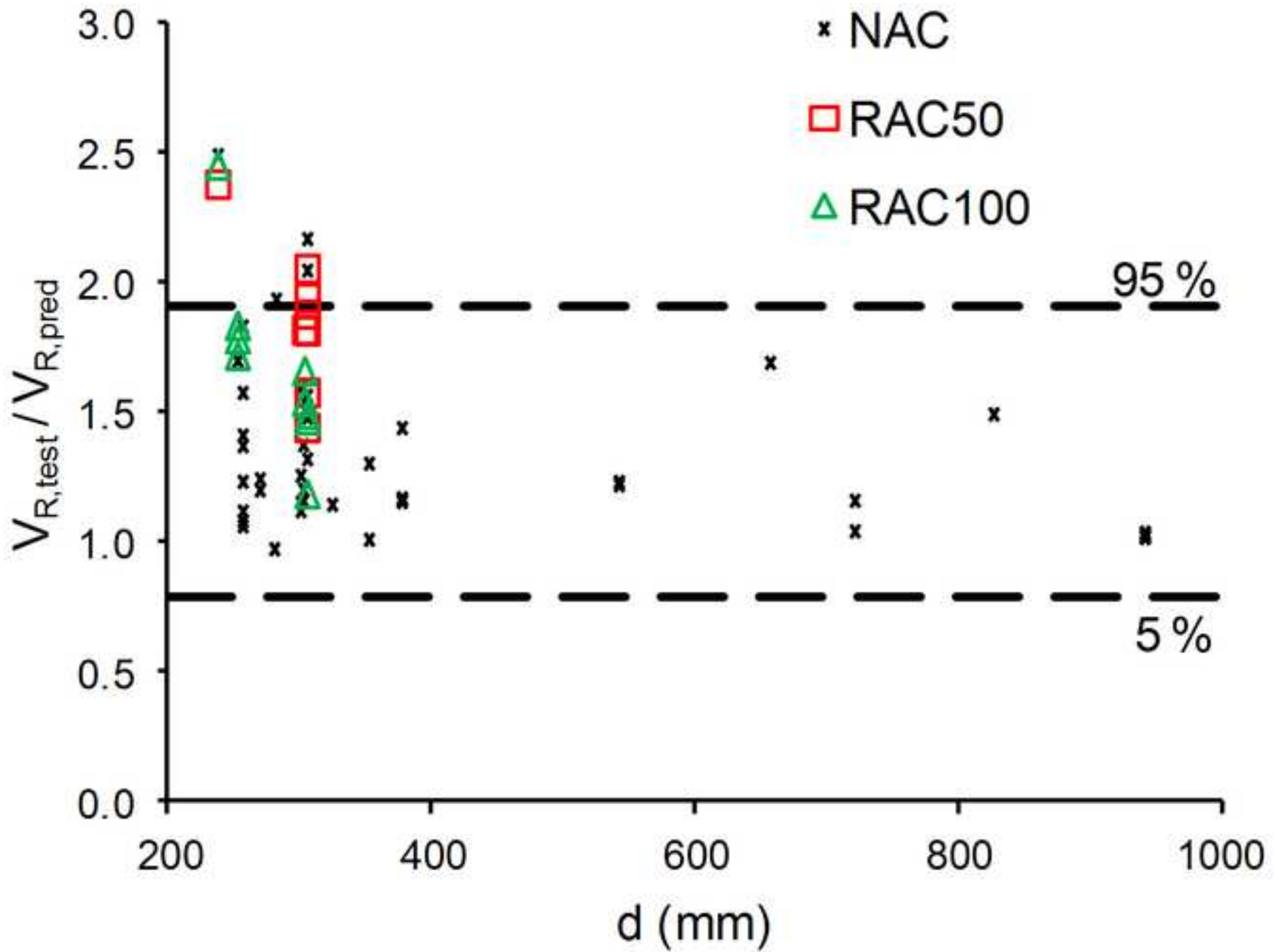
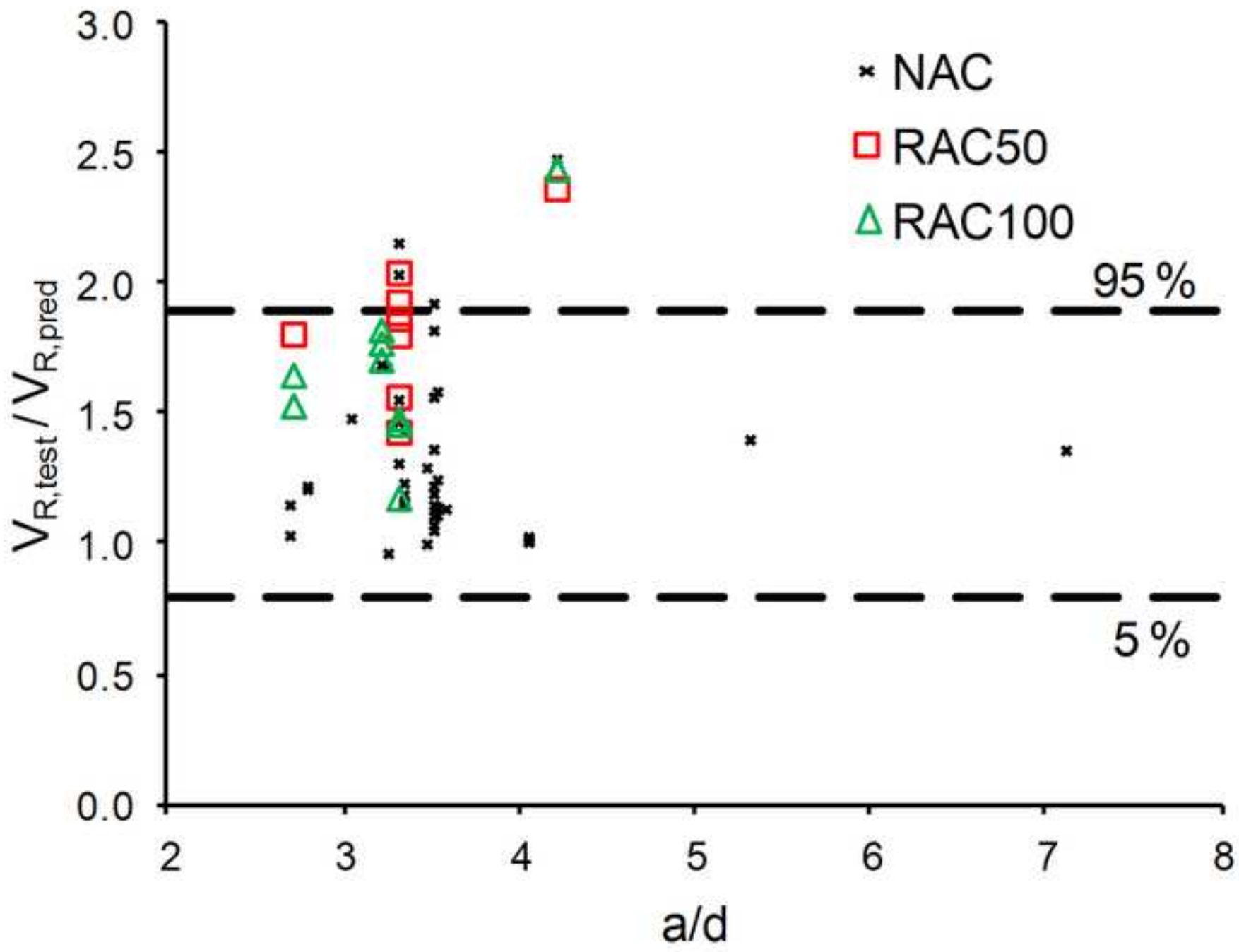


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Appendix A - Supplementary material

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1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
Author	Specimen	coarse RCA (%)	d_{max} (mm)	b (mm)	h (mm)	d (mm)	a/d	ρ_l (%)	ρ_w (%)	f_{yt} (MPa)	f_{yw} (MPa)	f_c (MPa)	$V_{R,test}$ (kN)	$M_{R,test}$ (kNm)	$I_{b,prov}$ (mm)	$I_{b,req}$ (mm)	β_{lb} (-)	$M_{R,pred}$ (kNm)	β_{pl} (-)	$V_{R,c}$ (kN)	$V_{R,s}$ (kN)	$V_{R,pred}$ (kN)	$V_{R,max}$ (kN)	$\beta_{sh}(-)$	$\Delta\beta = \beta_{sh}-\beta_{pl}$	Database selection
Han et al. (2001)	R3.0-N	100	25	170	300	270	3.0	1.1	-	430	-	31.2	55.1	44.6	150	37.1	0.25	54.1	0.83	44.7	0.0	44.7	298.6	1.23	0.41	Shear NS
Han et al. (2001)	R4.0-N	100	25	170	300	270	4.0	1.1	-	430	-	31.9	50.9	55.0	150	33.8	0.23	54.2	1.02	39.8	0.0	39.8	323.3	1.28	0.26	None
Etxeberria (2004)	HR50-1	50	25	200	350	303	3.3	2.98	-	500	-	41.34	89	89.0	225	34.2	0.15	222.9	0.40	92.5	0.0	92.5	402.0	0.96	0.56	Shear NS
Etxeberria (2004)	HR50-2	50	25	200	350	303	3.3	2.98	(Φ6/13) 0.22	500	544	41.34	220	220.0	225	105.7	0.47	222.9	0.99	31.1	110.4	141.5	506.1	1.55	0.57	Shear S
Etxeberria (2004)	HR50-3	50	25	200	350	303	3.3	2.98	(Φ6/17) 0.17	500	544	41.34	176	176.0	225	84.5	0.38	222.9	0.79	39.4	91.8	131.2	473.7	1.34	0.55	Shear S
Etxeberria (2004)	HR50-4	50	25	200	350	303	3.3	2.98	(Φ6/24) 0.12	500	544	41.34	164	164.0	225	78.8	0.35	222.9	0.74	42.1	66.6	108.7	464.3	1.51	0.77	Shear S
Etxeberria (2004)	HR100-1	100	25	200	350	303	3.3	2.98	-	500	-	39.75	84	84.0	225	33.1	0.15	220.9	0.38	92.7	0.0	92.7	387.4	0.91	0.53	Shear NS
Etxeberria (2004)	HR100-2	100	25	200	350	303	3.3	2.98	(Φ6/13) 0.22	500	544	39.75	189.5	189.5	225	93.4	0.42	220.9	0.86	35.3	117.0	152.2	471.4	1.24	0.39	Shear S
Etxeberria (2004)	HR100-3	100	25	200	350	303	3.3	2.98	(Φ6/17) 0.17	500	544	39.75	163	163.0	225	80.4	0.36	220.9	0.74	41.0	94.2	135.2	451.6	1.21	0.47	Shear S
Etxeberria (2004)	HR100-4	100	25	200	350	303	3.3	2.98	(Φ6/24) 0.12	500	544	39.75	168	168.0	225	82.8	0.37	220.9	0.76	39.8	66.1	105.9	455.4	1.59	0.83	Shear S
Etxeberria (2004)	HC-1	0	25	200	350	303	3.3	2.98	-	500	-	41.9	100.5	100.5	225	38.3	0.17	223.6	0.45	88.7	0.0	88.7	415.7	1.13	0.68	Shear NS
Etxeberria (2004)	HC-2	0	25	200	350	303	3.3	2.98	(Φ6/13) 0.22	500	544	41.9	213	213.0	225	101.4	0.45	223.6	0.95	32.7	111.8	144.6	505.6	1.47	0.52	Shear S
Etxeberria (2004)	HC-3	0	25	200	350	303	3.3	2.98	(Φ6/17) 0.17	500	544	41.9	177	177.0	225	84.3	0.37	223.6	0.79	39.7	91.7	131.3	478.7	1.35	0.56	Shear S
Etxeberria (2004)	HC-4	0	25	200	350	303	3.3	2.98	(Φ6/24) 0.12	500	544	41.9	187.5	187.5	225	89.3	0.40	223.6	0.84	37.4	63.6	101.1	486.8	1.86	1.02	Shear S
Sato et al. (2004)	CR45-03-WB	100	150	200	160	160	4.4	1.06	-	331	-	46.5	21.0	14.8	300	21.5	0.07	13.5	1.10	29.4	0.0	29.4	208.1	0.72	-0.38	Flexural
Sato et al. (2004)	CR60-03-WB	100	150	200	160	160	4.4	1.06	-	331	-	32.9	21.7	15.3	300	28.0	0.09	13.3	1.15	24.3	0.0	24.3	166.9	0.90	-0.26	None
Sato et al. (2004)	CREX45-03-WB	100	150	200	160	160	4.4	1.06	-	331	-	46.6	21.4	15.1	300	21.9	0.07	13.5	1.12	29.1	0.0	29.1	209.7	0.74	-0.38	Flexural
Sato et al. (2004)	CR45-01-10WB	100	150	200	160	160	4.4	0.59	-	331	-	30.4	12.1	8.5	300	22.7	0.08	8.0	1.06	24.2	0.0	24.2	155.4	0.50	-0.56	Flexural
Sato et al. (2004)	CR45-01-10DB	100	150	200	160	160	4.4	0.59	-	331	-	28.4	12.6	8.9	300	24.9	0.08	8.0	1.11	22.8	0.0	22.8	147.8	0.56	-0.56	Flexural
Sato et al. (2004)	CR60-01-10WB	100	150	200	160	160	4.4	0.59	-	331	-	34.5	13.2	9.3	300	22.8	0.08	8.1	1.16	24.5	0.0	24.5	173.7	0.54	-0.61	Flexural
Sato et al. (2004)	CR60-01-10DB	100	150	200	160	160	4.4	0.59	-	331	-	31.8	13.5	9.5	300	24.6	0.08	8.0	1.18	23.2	0.0	23.2	165.5	0.58	-0.60	Flexural
Sato et al. (2004)	CR45-01-13WB	100	150	200	160	160	4.4	1.06	-	331	-	30.4	19.7	13.9	300	26.9	0.09	13.2	1.05	24.6	0.0	24.6	153.9	0.80	-0.25	None
Sato et al. (2004)	CR45-01-13DB	100	150	200	160	160	4.4	1.06	-	331	-	28.4	20.0	14.1	300	28.5	0.10	13.1	1.07	23.6	0.0	23.6	145.0	0.85	-0.23	None
Sato et al. (2004)	CR60-01-13WB	100	150	200	160	160	4.4	1.06	-	331	-	34.5	20.0	14.1	300	25.0	0.08	13.3	1.06	26.0	0.0	26.0	168.2	0.77	-0.29	None
Sato et al. (2004)	CR60-01-13DB	100	150	200	160	160	4.4	1.06	-	331	-	31.8	21.4	15.1	300	28.3	0.09	13.2	1.14	24.0	0.0	24.0	162.5	0.89	-0.25	None
Sato et al. (2004)	CR45-01-16WB	100	150	200	160	160	4.4	1.65	-	342	-	30.4	27.3	19.2	300	29.3	0.10	19.9	0.97	25.9	0.0	25.9	150.0	1.05	0.09	None
Sato et al. (2004)	CR45-01-16DB	100	150	200	160	160	4.4	1.65	-	342	-	28.4	27.7	19.5	300	31.2	0.10	19.7	0.99	24.8	0.0	24.8	141.3	1.12	0.13	None
Sato et al. (2004)	CR60-01-16WB	100	150	200	160	160	4.4	1.65	-	342	-	34.5	28.3	19.9	300	27.9	0.09	20.1	0.99	27.1	0.0	27.1	164.8	1.04	0.06	None
Sato et al. (2004)	CR60-01-16DB	100	150	200	160	160	4.4	1.65	-	342	-	31.8	31.1	21.9	300	32.5	0.11	20.0	1.10	24.6	0.0	24.6	160.5	1.26	0.17	None
Sato et al. (2004)	V45-03-WB	0	150	200	160	160	4.4	1.06	-	331	-	57	21.3	15.0	300	19.1	0.06	13.6	1.10	32.3	0.0	32.3	239.3	0.66	-0.44	Flexural
Sato et al. (2004)	V60-03-WB	0	150	200	160	160	4.4	1.06	-	331	-	40.2	22.4	15.8	300	25.3	0.08	13.4	1.18	26.3	0.0	26.3	192.6	0.85	-0.33	None
Sato et al. (2004)	VEX45-03-WB	0	150	200	160	160	4.4	1.06	-	331	-	55.3	21.7	15.3	300	19.8	0.07	13.6	1.13	31.5	0.0	31.5	235.9	0.69	-0.44	Flexural
Sato et al. (2004)	V-01-10WB	0	150	200	160	160	4.4	0.59	-	331	-	30.6	11.4	8.0	300	21.3	0.07	8.0	1.00	25.1	0.0	25.1	153.4	0.45	-0.55	Flexural
Sato et al. (2004)	V-01-10DB	0	150	200	160	160	4.4	0.59	-	331	-	32.5	12.9	9.1	300	23.2	0.08	8.0	1.13	24.0	0.0	24.0	165.8	0.54	-0.59	Flexural
Sato et al. (2004)	V-01-13WB	0	150	200	160	160	4.4	1.06	-	331	-	30.6	19.5	13.7	300	26.4	0.09	13.2	1.04	24.9	0.0	24.9	154.0	0.78	-0.26	None
Sato et al. (2004)	V-01-13DB	0	150	200	160	160	4.4	1.06	-	331	-	32.5	19.9	14.0	300	25.9	0.09	13.2	1.06	25.4	0.0	25.4	161.3	0.78	-0.27	None
Sato et al. (2004)	V-01-16WB	0	150	200	160	160	4.4	1.65	-	342	-	30.6	27.6	19.4	300	29.5	0.10	19.9	0.98	25.8	0.0	25.8	151.1	1.07	0.09	None
Sato et al. (2004)	V-01-16DB	0	150	200	160	160	4.4	1.65	-	342	-	32.5	27.7	19.5	300	28.5	0.09	20.0	0.97	26.6	0.0	26.6	157.5	1.04	0.07	None
Gonzalez-Fonteboa and Martinez-Abella (2007)	V0RC	50	25	200	350	303	3.3	2.98	-	571	-	39.7	90.6	90.6	178	35.8	0.20	243.6	0.37	90.0	0.0	90.0	392.7	1.01	0.63	Shear NS
Gonzalez-Fonteboa and Martinez-Abella (2007)	V24RC	50	25	200	350	303	3.3	2.98	(Φ6/24) 0.12	571	500	39.3	164.3	164.3	178	81.6	0.46	242.9	0.68	40.2	61.2	101.4	449.2	1.62	0.94	Shear S
Gonzalez-Fonteboa and Martinez-Abella (2007)	V17RC	50	25	200	350	303	3.3	2.98	(Φ6/17) 0.17	571	500	41.5	177	177.0	178	84.8	0.48	246.6	0.72	39.3	84.2	123.6	475.7	1.43	0.71	Shear S
Gonzalez-Fonteboa and Martinez-Abella (2007)	V13RC	50	25	200	350	303	3.3	2.98	(Φ6/13) 0.22	571	500	40.5	233.6	233.6	178	113.7	0.64	245.0	0.95	28.4	98.9	127.3	508.5	1.83	0.88	Shear S
Gonzalez-Fonteboa and Martinez-Abella (2007)	V0CC	0	25	200	350	303	3.3	2.98	-	571	-	40.2	88.9	88.9	178	34.8	0.20	244.5	0.36	91.2	0.0	91.2	394.5	0.97	0.61	Shear NS
Gonzalez-Fonteboa and Martinez-Abella (2007)	V24CC	0	25	200	350	303	3.3	2.98	(Φ6/24) 0.12	571	500	39.2	128	128.0	178	63.7	0.36	242.7	0.53	50.0	65.9	115.9	420.1	1.10	0.58	Shear S
Gonzalez-Fonteboa and Martinez-Abella (2007)	V17CC	0	25	200	350	303	3.3	2.98	(Φ6/17) 0.17	571	500	39.1	150.8	150.8	178	75.2	0.42	242.6	0.62	43.4	88.7	132.1	437.3	1.14	0.52	Shear S
Gonzalez-Fonteboa and Martinez-Abella (2007)	V13CC	0	25	200	350	303	3.3	2.98	(Φ6/13) 0.22	571	500	37.7	190.3	190.3	178	97.2	0.55	240.0	0.79	33.4	107.3	140.7	455.6	1.35	0.56	Shear S
Ajdukiewicz and Kliszczewicz (2007)	ORN-1b1	100	16	200	300	250	3.2	0.9	(Φ6/10) 0.28	483	234.1	34.6	64	51.2	90	52.1	0.58	51.1	1.00	32.2	48.4	80.6	384.6	0.79	-0.21	None
Ajdukiewicz and Kliszczewicz (2007)	ORN-mb1	100	16	200	300	250	3.2	0.9	(Φ6/10) 0.28	483	234.1	56.4	78	62.4	90	45.8	0.51	52.5								

Study information		Aggregate information		Section properties			Loading and reinforcement			Material properties			Test results		Anchorage check			Bending check		Shear check					Database selection		
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	
Author	Specimen	coarse RCA (%)	d_{max} (mm)	b (mm)	h (mm)	d (mm)	a/d	ρ_l (%)	ρ_w (%)	f_{yt} (MPa)	f_{yw} (MPa)	f_c (MPa)	$V_{R,test}$ (kN)	$M_{R,test}$ (kNm)	$l_{b,prov}$ (mm)	$l_{b,req}$ (mm)	β_{lb} (-)	$M_{R,pred}$ (kNm)	β_{pl} (-)	$V_{R,c}$ (kN)	$V_{R,s}$ (kN)	$V_{R,pred}$ (kN)	$V_{R,max}$ (kN)	$\beta_{sh}(-)$	$\Delta\beta = \beta_{sh}-\beta_{pl}$	Database $\Delta_{cr}=0.35$	
Ajdukiewicz and Kliszczewicz (2007)	GRN-mb2	100	16	200	300	250	3.2	1.6	(Φ6/10) 0.28	448	234.1	59.6	118.5	94.8	90	37.8	0.42	84.5	1.12	38.9	47.5	86.5	559.7	1.37	0.25	None	
Ajdukiewicz and Kliszczewicz (2007)	BRN-lb2	100	16	200	300	250	3.2	1.6	(Φ6/10) 0.28	448	234.1	35.8	120.5	96.4	90	53.9	0.60	80.8	1.19	26.5	47.1	73.6	400.5	1.64	0.44	Shear S	
Ajdukiewicz and Kliszczewicz (2007)	BRN-mb2	100	16	200	300	250	3.2	1.6	(Φ6/10) 0.28	448	234.1	59.6	119	95.2	90	37.9	0.42	84.5	1.13	38.8	47.4	86.2	560.4	1.38	0.25	None	
Ajdukiewicz and Kliszczewicz (2007)	ONN-lb1	0	16	200	300	250	3.2	0.9	(Φ6/10) 0.28	483	234.1	37.7	64.5	51.6	90	49.6	0.55	51.4	1.00	33.8	48.2	82.0	408.2	0.79	-0.22	None	
Ajdukiewicz and Kliszczewicz (2007)	ONN-mb1	0	16	200	300	250	3.2	0.9	(Φ6/10) 0.28	483	234.1	57.9	80	64.0	90	46.2	0.51	52.5	1.22	37.2	43.3	80.5	581.0	0.99	-0.22	None	
Ajdukiewicz and Kliszczewicz (2007)	GNN-lb1	0	16	200	300	250	3.2	0.9	(Φ6/10) 0.28	483	234.1	39.8	78	62.4	90	57.8	0.64	51.6	1.21	30.1	43.9	74.0	449.0	1.05	-0.16	None	
Ajdukiewicz and Kliszczewicz (2007)	GNN-mb1	0	16	200	300	250	3.2	0.9	(Φ6/10) 0.28	483	234.1	58.3	70	56.0	90	40.2	0.45	52.5	1.07	41.4	46.4	87.8	560.0	0.80	-0.27	None	
Ajdukiewicz and Kliszczewicz (2007)	BNN-lb1	0	16	200	300	250	3.2	0.9	(Φ6/10) 0.28	483	234.1	40.1	75.5	60.4	90	55.7	0.62	51.6	1.17	31.0	44.7	75.7	446.8	1.00	-0.17	None	
Ajdukiewicz and Kliszczewicz (2007)	BNN-mb1	0	16	200	300	250	3.2	0.9	(Φ6/10) 0.28	483	234.1	61.8	73	58.4	90	40.4	0.45	52.7	1.11	41.5	45.5	87.0	589.9	0.84	-0.27	None	
Ajdukiewicz and Kliszczewicz (2007)	ONN-lb2	0	16	200	300	250	3.2	1.6	(Φ6/10) 0.28	448	234.1	38.2	113.5	90.8	90	48.6	0.54	81.4	1.12	29.4	48.5	77.9	410.5	1.46	0.34	None	
Ajdukiewicz and Kliszczewicz (2007)	ONN-mb2	0	16	200	300	250	3.2	1.6	(Φ6/10) 0.28	448	234.1	59.1	117	93.6	90	37.5	0.42	84.5	1.11	39.1	47.8	86.9	554.3	1.35	0.24	None	
Ajdukiewicz and Kliszczewicz (2007)	GNN-lb2	0	16	200	300	250	3.2	1.6	(Φ6/10) 0.28	448	234.1	38.7	108.5	86.8	90	46.1	0.51	81.5	1.06	30.9	49.4	80.4	408.3	1.35	0.29	None	
Ajdukiewicz and Kliszczewicz (2007)	BNN-lb2	0	16	200	300	250	3.2	1.6	(Φ6/10) 0.28	448	234.1	39.6	115.5	92.4	90	48.3	0.54	81.7	1.13	29.8	48.1	77.8	422.8	1.48	0.35	Shear S	
Ajdukiewicz and Kliszczewicz (2007)	BNN-mb2	0	16	200	300	250	3.2	1.6	(Φ6/10) 0.28	448	234.1	60.8	119	95.2	90	37.4	0.42	84.6	1.12	39.3	47.4	86.8	567.9	1.37	0.25	None	
Fathifazi et al. (2009)	EM-Min	63.5	19	200	304	304	2.6	0.49	(Φ10/20) 0.39	420	450	41.6	57.5	46.0	200	52.1	0.26	29.5	1.56	36.9	131.4	168.3	587.3	0.34	-1.22	Flexural	
Fathifazi et al. (2009)	EM-Av	63.5	19	200	304	304	2.7	1.99	(Φ15/20) 0.88	420	450	41.6	184.5	149.2	200	82.3	0.41	168.1	0.89	38.7	404.7	443.3	477.5	0.42	-0.47	Flexural	
Fathifazi et al. (2009)	EM-Max	63.5	19	200	304	304	2.6	3.26	(Φ15/10) 1.77	420	450	41.6	279.7	221.9	200	95.2	0.48	208.7	1.06	25.5	770.4	496.7	496.7	0.56	-0.50	Flexural	
Fathifazi et al. (2009)	EM-CMP	63.5	19	200	304	304	2.7	3.31	(Φ810) 1.01	420	530	41.6	305.5	246.1	200	102.4	0.51	208.7	1.18	22.2	247.5	269.7	512.6	1.13	-0.05	None	
Fathifazi et al. (2009)	EV-Min	74.3	19	200	304	304	2.6	0.49	(Φ10/20) 0.39	420	450	49.1	58.4	46.7	200	47.4	0.24	29.6	1.58	40.1	130.2	170.3	658.8	0.34	-1.24	Flexural	
Fathifazi et al. (2009)	EV-Av	74.3	19	200	304	304	2.7	1.99	(Φ15/20) 0.88	420	450	49.1	185.7	150.2	200	74.2	0.37	171.9	0.87	44.5	403.7	448.2	534.3	0.41	-0.46	Flexural	
Fathifazi et al. (2009)	EV-Max	74.3	19	200	304	304	2.6	3.26	(Φ15/10) 1.77	420	450	49.1	283.8	225.2	200	86.5	0.43	215.1	1.05	30.8	766.0	557.2	557.2	0.51	-0.54	Flexural	
Fathifazi et al. (2009)	EV-CMP	74.3	19	200	304	304	2.7	3.31	(Φ810) 1.01	420	530	49.1	305.0	245.7	200	91.6	0.46	215.1	1.14	27.9	247.7	275.5	572.2	1.11	-0.04	None	
Fathifazi et al. (2009)	CL-Av	0	19	200	304	304	2.6	1.99	(Φ15/20) 0.88	420	450	37.1	178.5	142.7	200	86.0	0.43	165.1	0.86	36.1	410.9	410.9	436.8	0.43	-0.43	Flexural	
Fathifazi et al. (2009)	CL-CMP	0	19	200	304	304	2.7	3.33	(Φ810) 1.01	420	530	37.1	283.3	229.1	200	101.9	0.51	203.6	1.13	21.1	254.8	275.9	464.7	1.03	-0.10	None	
Fathifazi et al. (2009)	CG-Av	0	19	200	304	304	2.6	1.99	(Φ15/20) 0.88	420	450	33.8	175.3	139.1	200	89.8	0.45	162.4	0.86	33.6	414.4	407.5	407.5	0.43	-0.43	Flexural	
Fathifazi et al. (2009)	CG-CMP	0	19	200	304	304	2.7	3.33	(Φ810) 1.01	420	530	33.8	281.2	226.5	200	107.6	0.54	199.0	1.14	18.4	256.0	274.4	435.2	1.02	-0.11	None	
Fathifazi et al. (2010)	EM-3S-R	63.5	19	200	375	306	2.6	2.46	(Φ8/20) 0.25	420	530	41.6	172	136.8	200	61.7	0.31	168.8	0.81	42.2	140.6	182.8	468.7	0.94	0.13	None	
Fathifazi et al. (2010)	EM-6S-R	63.5	19	200	375	306	2.6	3.2	(Φ8/10) 0.5	420	530	41.6	308	245.0	200	84.9	0.42	209.9	1.17	22.3	250.1	272.4	514.6	1.13	-0.04	None	
Fathifazi et al. (2010)	EM-6S-D	63.5	19	200	385	301	2.7	4	(Φ10/20) 0.5	420	530	41.6	341	277.1	200	76.4	0.38	241.2	1.15	17.8	197.4	215.1	496.1	1.59	0.44	Shear S	
Fathifazi et al. (2010)	EV-3S-R	74.3	19	200	385	301	2.7	2.46	(Φ8/20) 0.25	420	530	49.1	235	191.0	200	76.7	0.38	167.0	1.14	34.0	120.5	154.5	573.8	1.52	0.38	Shear S	
Fathifazi et al. (2010)	EV-6S-R	74.3	19	200	385	301	2.7	3.2	(Φ8/10) 0.5	420	530	49.1	308	250.3	200	77.3	0.39	209.3	1.20	26.6	240.2	266.9	575.1	1.15	-0.04	None	
Fathifazi et al. (2010)	EV-6S-D	74.3	19	200	385	301	2.7	4	(Φ10/20) 0.5	420	530	49.1	327	265.8	200	65.6	0.33	250.9	1.06	25.5	200.6	226.1	547.2	1.45	0.39	Shear S	
Fathifazi et al. (2010)	CL-M	0	19	200	375	309	2.6	1.62	-	420	-	-	38.8	92.8	74.6	200	41.9	0.21	118.2	0.63	74.8	0.0	74.8	427.8	1.24	0.61	Shear NS
Fathifazi et al. (2010)	CG-2.7	0	19	200	375	309	2.6	1.62	-	420	-	-	34.4	150	120.5	200	73.4	0.37	116.7	1.03	54.4	0.0	54.4	451.1	2.76	1.73	Shear NS
Fathifazi et al. (2010)	CL-6S-R	0	19	200	385	309	2.6	3.2	(Φ8/10) 0.5	420	530	38.8	287	230.6	200	82.1	0.41	211.0	1.09	23.1	260.9	284.0	484.1	1.01	-0.08	None	
Fathifazi et al. (2010)	CG-6S-R	0	19	200	385	309	2.6	3.2	(Φ8/10) 0.5	420	530	34.4	284	228.2	200	88.0	0.44	205.1	1.11	19.5	261.9	281.4	444.3	1.01	-0.10	None	
Choi et al. (2010)	RARAC50-H2.5	50	25	200	400	360	2.5	1.61	-	500	-	-	24.1	87.9	79.1	200	51.8	0.26	172.8	0.46	76.7	0.0	76.7	319.0	1.15	0.69	Shear NS
Choi et al. (2010)	RARAC50-H3.25	50	25	200	400	360	3.3	1.61	-	500	-	-	24.1	71.6	83.8	200	42.2	0.21	172.8	0.48	74.5	0.0	74.5	323.7	0.96	0.48	Shear NS
Choi et al. (2010)	RARAC50-L2.5	50	25	200	400	360	2.5	0.53	-	500	-	-	24.1	57.8	52.0	200	103.5	0.52	64.8	0.80	54.1	0.0	54.1	381.9	1.07	0.27	None
Choi et al. (2010)	RARAC50-M2.5	50	25	200	400	360	2.5	0.83	-	500	-	-	24.1	67.1	60.4	200	76.8	0.38	98.0	0.62	63.8	0.0	63.8	350.6	1.05	0.44	Shear NS
Choi et al. (2010)	RARAC100-H2.5	100	25	200	400	360	2.5	1.61	-	500	-	-	22.6	84.8	76.3	200	52.2	0.26	170.5	0.45	75.4	0.0	75.4	296.9	1.13	0.68	Shear NS
Choi et al. (2010)	RARAC100-H3.25	100	25	200	400	360	3.3	1.61	-	500	-	-	22.6	57.8	67.6	200	35.6	0.18	170.5	0.40	78.8	0.0	78.8	290.3	0.73	0.34	None
Choi et al. (2010)	RARAC100-L2.5	100	25	200	400	360	2.5	0.53	-	500	-	-	22.6	59.8	53.8	200	111.8	0.56	64.5	0.83	51.3	0.0	51.3	361.8	1.17	0.33	None
Choi et al. (2010)	RAC100-M2.5	100	25	200	400	360	2.5	0.83	-	500	-	-	22.6	70.1	63.1	200	83.7	0.42	97.4	0.65	60.4	0.0	60.4	332.7	1.16	0.51	Shear NS
Choi et al. (2010)	NANAC-H2.5	0	25	200	400	360	2.5	1.61	-	500	-	-	24.7	90.7	81.6	200	52.6	0.26	173.7	0.47	76.6	0.0	76.6	329.2	1.18	0.71	Shear NS
Choi et al. (2010)	NANAC-H3.25	0	25	200	400	360	3.3	1.61	-	500	-	-	24.7	71.1	83.2	200	41.2	0.21	173.7	0.48	75.7	0.0	75.7	331.2	0.94	0.46	Shear NS
Choi et al. (2010)	NANAC-L2.5	0																									

Study information		Aggregate information		Section properties			Loading and reinforcement			Material properties			Test results		Anchorage check		Bending check		Shear check				Database selection				
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	
Author	Specimen	coarse RCA d_{max} (%)		b (mm)	h (mm)	d (mm)	a/d	ρ_l (%)	ρ_w (%)	f_{yt} (MPa)	f_{yw} (MPa)	f_c (MPa)	$V_{R,test}$ (kN)	$M_{R,test}$ (kNm)	$I_{b,prov}$ (mm)	$I_{b,req}$ (mm)	β_{lb} (-)	$M_{R,prod}$ (kNm)	β_{pl} (-)	$V_{R,c}$ (kN)	$V_{R,s}$ (kN)	$V_{R,kn}$ (kN)	$V_{R,max}$ (kN)	$\beta_{sh}(-)$	$\Delta\beta = \beta_{sh}-\beta_{pl}$	Database	$\Delta_{cr}=0.35$
Ignjatovic et al. (2013)	RAC50-1a	50	31.5	200	300	268	4.2	0.28	($\Phi 8/15$) 0.34	640	555	35.36	27	27.0	250	43.3	0.17	25.2	1.07	27.7	109.1	136.8	486.7	0.20	-0.87	Flexural	
Ignjatovic et al. (2013)	RAC50-2a	50	31.5	200	300	263	4.2	1.46	($\Phi 10/7.5$) 1.05	550	555	35.36	110.55	110.6	250	77.9	0.31	97.6	1.13	25.3	382.8	408.1	450.6	0.27	-0.86	Flexural	
Ignjatovic et al. (2013)	RAC50-3a	50	31.5	200	300	244	4.2	2.54	($\Phi 10/6$) 1.31	550	555	35.36	160.35	160.4	250	70.0	0.28	135.2	1.19	20.5	479.0	400.8	400.8	0.40	-0.79	Flexural	
Ignjatovic et al. (2013)	RAC100-1a	100	31.5	200	300	268	4.2	0.28	($\Phi 8/15$) 0.34	640	555	34	26.8	26.8	250	44.1	0.18	25.2	1.07	27.3	109.7	137.0	473.2	0.20	-0.87	Flexural	
Ignjatovic et al. (2013)	RAC100-2a	100	31.5	200	300	263	4.2	1.46	($\Phi 10/7.5$) 1.05	550	555	34	105.4	105.4	250	76.3	0.31	97.1	1.09	25.7	393.3	419.0	432.8	0.25	-0.83	Flexural	
Ignjatovic et al. (2013)	RAC100-3a	100	31.5	200	300	244	4.2	2.54	($\Phi 10/6$) 1.31	550	555	34	142.6	142.6	250	63.9	0.26	133.7	1.07	22.5	507.5	376.4	376.4	0.38	-0.69	Flexural	
Ignjatovic et al. (2013)	NAC1a	0	31.5	200	300	268	4.2	0.28	($\Phi 8/15$) 0.34	640	555	34.96	28.35	28.4	250	45.8	0.18	25.2	1.13	26.5	105.4	131.9	488.5	0.21	-0.91	Flexural	
Ignjatovic et al. (2013)	NAC2a	0	31.5	200	300	263	4.2	1.46	($\Phi 10/7.5$) 1.05	550	555	34.96	108.55	108.6	250	77.1	0.31	97.5	1.11	25.5	386.8	412.4	444.8	0.26	-0.85	Flexural	
Ignjatovic et al. (2013)	NAC3a	0	31.5	200	300	244	4.2	2.54	($\Phi 10/6$) 1.31	550	555	34.96	137.6	137.6	250	60.6	0.24	134.8	1.02	24.0	516.0	379.3	379.3	0.36	-0.66	Flexural	
Ignjatovic (2013)	RAC50-1b	50	31.5	200	300	235	4.2	4.09	-	555	-	33.44	91.8	90.6	250	26.2	0.10	163.3	0.55	61.8	0.0	61.8	283.2	1.49	0.93	Shear NS	
Ignjatovic (2013)	RAC50-3b	50	31.5	200	300	235	4.2	4.09	($\Phi 6/15$) 0.19	555	300	33.44	156.9	154.9	250	56.1	0.22	163.3	0.95	21.8	43.4	65.2	325.5	2.41	1.46	Shear S	
Ignjatovic (2013)	RAC100-1b	100	31.5	200	300	235	4.2	4.09	-	555	-	34.48	104.8	103.4	250	29.4	0.12	165.9	0.62	59.1	0.0	59.1	298.1	1.77	1.15	Shear NS	
Ignjatovic (2013)	RAC100-3b	100	31.5	200	300	235	4.2	4.09	($\Phi 6/15$) 0.19	555	300	34.48	163.4	161.3	250	57.2	0.23	165.9	0.97	21.4	42.8	64.2	336.2	2.55	1.57	Shear S	
Ignjatovic (2013)	NAC1b	0	31.5	200	300	235	4.2	4.09	-	555	-	30.8	106.3	104.9	250	32.1	0.13	155.8	0.67	55.5	0.0	55.5	277.4	1.92	1.24	Shear NS	
Ignjatovic (2013)	NAC3b	0	31.5	200	300	235	4.2	4.09	($\Phi 6/15$) 0.19	555	300	30.8	159.9	157.8	250	60.4	0.24	155.8	1.01	19.3	43.1	62.4	309.9	2.56	1.55	Shear S	
Kim et al. (2013)	RF-S2	100	25	200	350	300	2.5	1.94	-	651	-	34.9	72.9	54.7	150	33.5	0.22	184.7	0.30	85.7	0.0	85.7	352.4	0.85	0.55	Shear NS	
Kim et al. (2013)	RF-M2	100	25	200	530	450	2.5	1.93	-	610	-	34.9	96.4	108.5	150	29.7	0.20	393.7	0.28	123.6	0.0	123.6	517.3	0.78	0.50	Shear NS	
Kim et al. (2013)	RF-L2	100	25	200	680	600	2.5	1.94	-	651	-	34.9	125.1	187.7	150	28.8	0.19	738.9	0.25	154.3	0.0	154.3	686.0	0.81	0.56	Shear NS	
Kim et al. (2013)	RF-M3	100	25	300	530	450	2.5	2.00	-	600	-	34.9	159.8	179.8	150	31.7	0.21	599.2	0.30	181.2	0.0	181.2	784.8	0.88	0.58	Shear NS	
Kim et al. (2013)	RF-L4	100	25	400	680	600	2.5	1.94	-	651	-	34.9	256.6	384.9	150	29.5	0.20	1477.8	0.26	305.9	0.0	305.9	1377.9	0.84	0.58	Shear NS	
Kim et al. (2013)	RH-S2	50	25	200	350	300	2.5	1.94	-	651	-	32.6	60.6	45.5	150	29.2	0.19	181.8	0.25	88.5	0.0	88.5	325.1	0.69	0.43	Shear NS	
Kim et al. (2013)	RH-M2	50	25	200	530	450	2.5	1.93	-	610	-	32.6	108.9	122.5	150	35.1	0.23	387.9	0.32	114.3	0.0	114.3	505.2	0.95	0.64	Shear NS	
Kim et al. (2013)	RH-L2	50	25	200	680	600	2.5	1.94	-	651	-	32.6	126.1	189.2	150	30.3	0.20	727.0	0.26	148.7	0.0	148.7	656.4	0.85	0.59	Shear NS	
Kim et al. (2013)	RH-M3	50	25	300	530	450	2.5	2.00	-	600	-	32.6	154.2	173.5	150	32.0	0.21	590.2	0.29	177.4	0.0	177.4	745.2	0.87	0.58	Shear NS	
Kim et al. (2013)	RH-L4	50	25	400	680	600	2.5	1.94	-	651	-	32.6	261.5	392.3	150	31.5	0.21	1454.0	0.27	293.7	0.0	293.7	1321.0	0.89	0.62	Shear NS	
Kim et al. (2013)	NA-S2	0	25	200	350	300	2.5	1.94	-	651	-	31.8	75.5	56.6	150	36.9	0.25	180.6	0.31	80.8	0.0	80.8	333.5	0.93	0.62	Shear NS	
Kim et al. (2013)	NA-M2	0	25	200	530	450	2.5	1.93	-	610	-	31.8	106.9	120.3	150	35.0	0.23	385.6	0.31	113.7	0.0	113.7	495.2	0.94	0.63	Shear NS	
Kim et al. (2013)	NA-L2	0	25	200	680	600	2.5	1.94	-	651	-	31.8	125.9	188.9	150	30.8	0.21	722.5	0.26	146.9	0.0	146.9	645.5	0.86	0.60	Shear NS	
Kim et al. (2013)	NA-M3	0	25	300	530	450	2.5	2.00	-	600	-	31.8	156.7	176.3	150	33.0	0.22	586.7	0.30	174.2	0.0	174.2	735.0	0.90	0.60	Shear NS	
Kim et al. (2013)	NA-L4	0	25	400	680	600	2.5	1.94	-	651	-	31.8	256.4	384.6	150	31.4	0.21	1445.0	0.27	292.1	0.0	292.1	1294.9	0.88	0.61	Shear NS	
Knaack and Kurama (2014)	S50-1a	50	19	150	230	200	3.8	1.3	-	570	-	43.6	44	33.4	200	37.8	0.19	40.6	0.82	30.0	0.0	30.0	265.1	1.47	0.64	Shear NS	
Knaack and Kurama (2014)	S50-1b	50	19	150	230	200	3.8	1.3	-	570	-	43.6	39.1	29.7	200	33.6	0.17	40.6	0.73	32.2	0.0	32.2	255.7	1.21	0.48	Shear NS	
Knaack and Kurama (2014)	S50-2a	50	19	150	230	200	3.8	1.3	-	570	-	40.2	43.7	33.2	200	39.6	0.20	40.2	0.83	28.9	0.0	28.9	250.6	1.51	0.69	Shear NS	
Knaack and Kurama (2014)	S50-2b	50	19	150	230	200	3.8	1.3	-	570	-	40.2	41.2	31.3	200	37.3	0.19	40.2	0.78	30.0	0.0	30.0	246.1	1.38	0.60	Shear NS	
Knaack and Kurama (2014)	S100-1a	100	19	150	230	200	3.8	1.3	-	570	-	41.4	36.4	27.7	200	32.4	0.16	40.4	0.69	32.7	0.0	32.7	241.8	1.11	0.43	Shear NS	
Knaack and Kurama (2014)	S100-1b	100	19	150	230	200	3.8	1.3	-	570	-	41.4	38	28.9	200	33.8	0.17	40.4	0.72	31.9	0.0	31.9	244.9	1.19	0.48	Shear NS	
Knaack and Kurama (2014)	S100-2a	100	19	150	230	200	3.8	1.3	-	570	-	35.7	39.9	30.3	200	39.1	0.20	39.7	0.76	28.8	0.0	28.8	225.2	1.39	0.62	Shear NS	
Knaack and Kurama (2014)	S100-2b	100	19	150	230	200	3.8	1.3	-	570	-	35.7	36.1	27.4	200	35.4	0.18	39.7	0.69	30.5	0.0	30.5	218.5	1.18	0.49	Shear NS	
Knaack and Kurama (2014)	S0-1a	0	19	150	230	200	3.8	1.3	-	570	-	32.6	31.1	23.6	200	32.4	0.16	39.3	0.60	31.7	0.0	31.7	197.0	0.98	0.38	Shear NS	
Knaack and Kurama (2014)	S0-1b	0	19	150	230	200	3.8	1.3	-	570	-	32.6	36.9	28.0	200	38.5	0.19	39.3	0.71	28.8	0.0	28.8	207.0	1.28	0.57	Shear NS	
Knaack and Kurama (2014)	S0-2a	0	19	150	230	200	3.8	1.3	-	570	-	50.3	40.4	30.7	200	31.5	0.16	41.1	0.75	33.9	0.0	33.9	284.1	1.19	0.44	Shear NS	
Knaack and Kurama (2014)	S0-2b	0	19	150	230	200	3.8	1.3	-	570	-	50.3	42.3	32.1	200	33.0	0.17	41.1	0.78	33.0	0.0	33.0	288.1	1.28	0.50	Shear NS	
Knaack and Kurama (2014)	F50-1a	50	19	150	230	200	3.8	1.3	($\Phi 10/9.5$) 1.10	572	420	40	55.0	41.8	200	62.5	0.31	41.5	1.01	18.0	189.7	207.7	265.8	0.26	-0.74	Flexural	
Knaack and Kurama (2014)	F50-1b	50	19	150	230	200	3.8	1.3	($\Phi 10/9.5$) 1.10	572	420	40	56.7	43.1	200	64.5	0.32	41.5	1.04	17.5	186.7	204.2	268.3	0.28	-0.76	Flexural	
Knaack and Kurama (2014)	F50-2a	50	19	150	230	200	3.8	1.3	($\Phi 10/9.5$) 1.10	572	420	39.3	54.3	41.3	200	62.5	0.31	41.4	1.00	18.0	190.8	208.8	261.7	0.26	-0.74	Flexural	
Knaack and Kurama (2014)	F50-2b	50	19	150	230	200	3.8	1.3	($\Phi 10/9.5$) 1.10	572	420	39.3	54.3	41.3	200	62.5	0.31	41.4	1.00	18.0	190.8	208.8	261.7	0.26	-0.74	Flexural	
Knaack and Kurama (2014)	F100-1a	100	19	150	230	200	3.8	1.3																			

Study information		Aggregate information		Section properties			Loading and reinforcement			Material properties			Test results		Anchorage check			Bending check		Shear check				Database selection		
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
Author	Specimen	coarse RCA (%)	d_{max} (mm)	b (mm)	h (mm)	d (mm)	a/d	ρ_l (%)	ρ_w (%)	f_{yt} (MPa)	f_{yw} (MPa)	f_c (MPa)	$V_{R,test}$ (kN)	$M_{R,test}$ (kNm)	$l_{b,prov}$ (mm)	$l_{b,req}$ (mm)	β_{lb} (-)	$M_{R,pred}$ (kNm)	β_{fl} (-)	$V_{R,c}$ (kN)	$V_{R,s}$ (kN)	$V_{R,pred}$ (kN)	$V_{R,max}$ (kN)	$\beta_{sh}(-)$	$\Delta\beta = \beta_{sh}-\beta_{fl}$	Database $\Delta_{cr}=0.35$
Arezoumandi et al. (2015)	RAC50 NS-8 2	50	25	300	460	375	3.2	2.71	-	450	-	35.5	168.7	202.4	250	29.2	0.12	423.7	0.48	147.7	0.0	147.7	685.6	1.14	0.66	Shear NS
Arezoumandi et al. (2015)	NAC NS-4 1	0	25	300	460	400	3.0	1.27	-	450	-	37.3	121.2	145.4	250	40.6	0.16	252.7	0.58	139.8	0.0	139.8	808.1	0.87	0.29	None
Arezoumandi et al. (2015)	NAC NS-6 1	0	25	300	460	375	3.2	2.03	-	450	-	37.3	143.2	171.8	250	32.0	0.13	336.9	0.51	143.7	0.0	143.7	727.8	1.00	0.49	Shear NS
Arezoumandi et al. (2015)	NAC NS-8 1	0	25	300	460	375	3.2	2.71	-	450	-	37.3	173.5	208.2	250	29.1	0.12	428.0	0.49	149.7	0.0	149.7	712.7	1.16	0.67	Shear NS
Arezoumandi et al. (2015)	NAC NS-4 2	0	25	300	460	400	3.0	1.27	-	450	-	34.2	129.9	155.9	250	46.1	0.18	250.8	0.62	129.4	0.0	129.4	776.1	1.00	0.38	Shear NS
Arezoumandi et al. (2015)	NAC NS-6 2	0	25	300	460	375	3.2	2.03	-	450	-	34.2	167	200.4	250	39.6	0.16	332.5	0.60	128.3	0.0	128.3	712.0	1.30	0.70	Shear NS
Arezoumandi et al. (2015)	NAC NS-8 2	0	25	300	460	375	3.2	2.71	-	450	-	34.2	170.8	205.0	250	30.3	0.12	420.2	0.49	144.3	0.0	144.3	670.5	1.18	0.70	Shear NS

Annotations:

d_{max} - maximum aggregate size	$M_{R,test}$ - measured flexural strength
b - cross-section width	$l_{b,prov}$ - provided anchorage length
h - cross-section height	$l_{b,req}$ - required anchorage length
d - effective cross-section height	β_{lb} - provided-to-required anchorage length ratio
a/d - shear span-to-height ratio	$M_{R,pred}$ - predicted flexural strength
ρ_l - longitudinal reinforcement ratio	β_{fl} - measured-to-predicted flexural strength ratio
ρ_w - transverse reinforcement ratio	$V_{R,c}$ - predicted shear strength attributed to concrete
f_{yt} - longitudinal reinforcement yield stress	$V_{R,s}$ - predicted shear strength attributed to transverse reinforcement
f_{yw} - transverse reinforcement yield stress	$V_{R,pred}$ - predicted shear strength
f_c - concrete compressive strength	$V_{R,max}$ - limit for predicted shear strength
$V_{R,test}$ - measured shear strength	β_{sh} - measured-to-predicted shear strength ratio